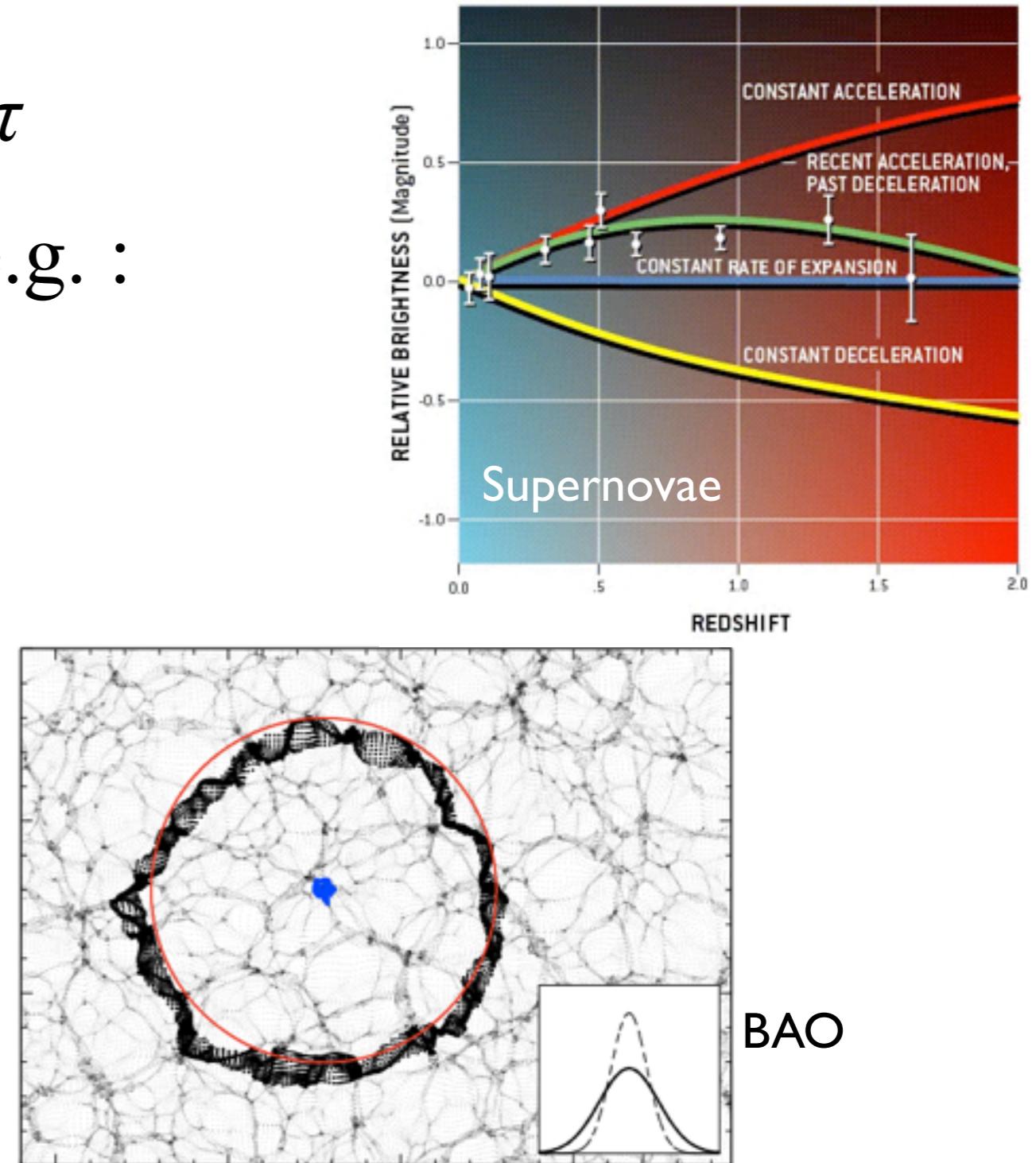
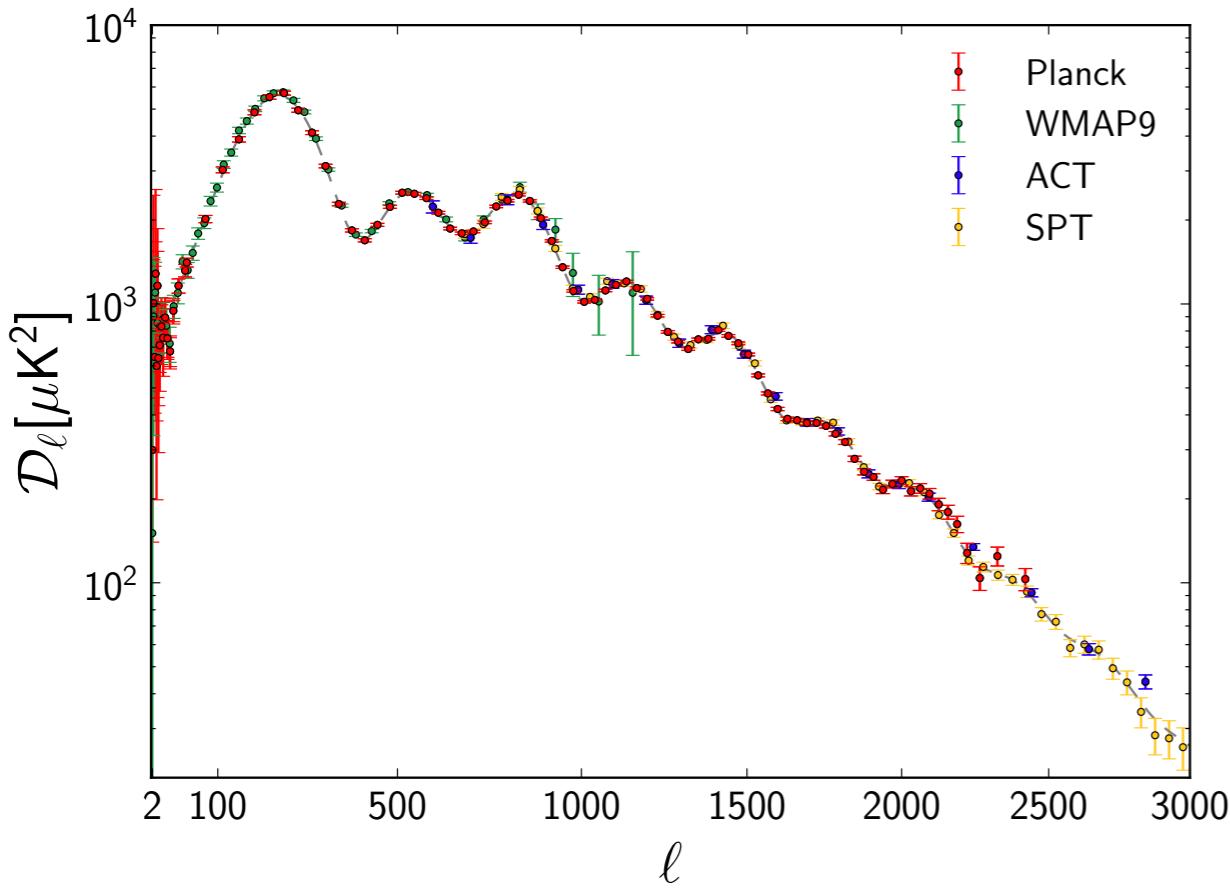
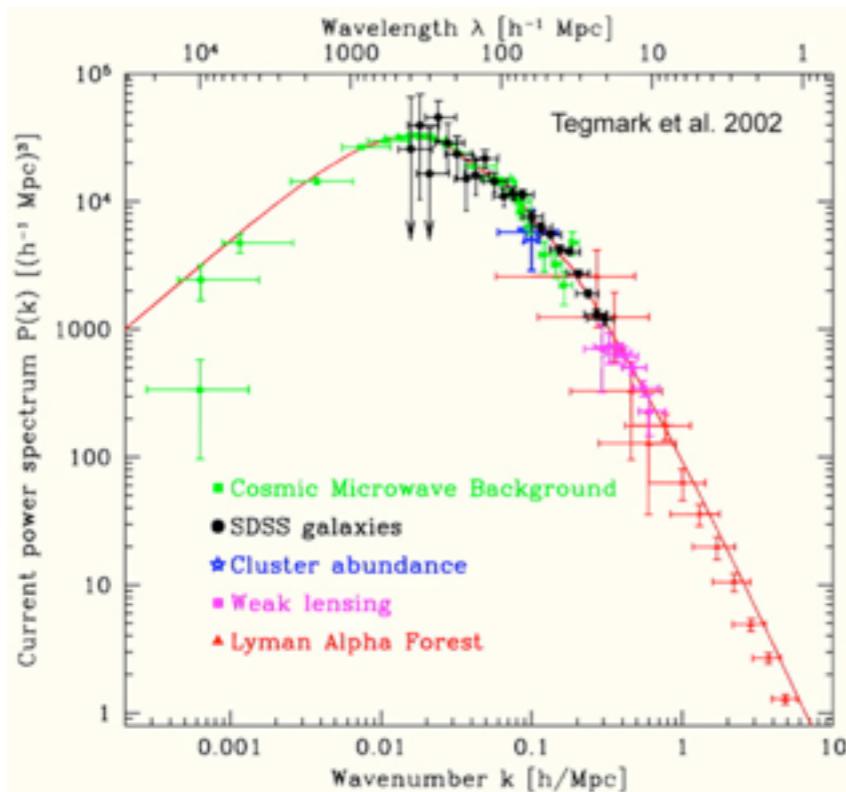


The Standard Model (of Cosmology): Λ CDM

- $H_0, \Omega_b, \Omega_m, \Lambda, \sigma_8, n_s, \tau$
- fits a wealth of data, e.g. :



small-scale structure



Millennium-2 simulation (Boylan-Kolchin et al.)

small-scale $P(k)$ is interesting!

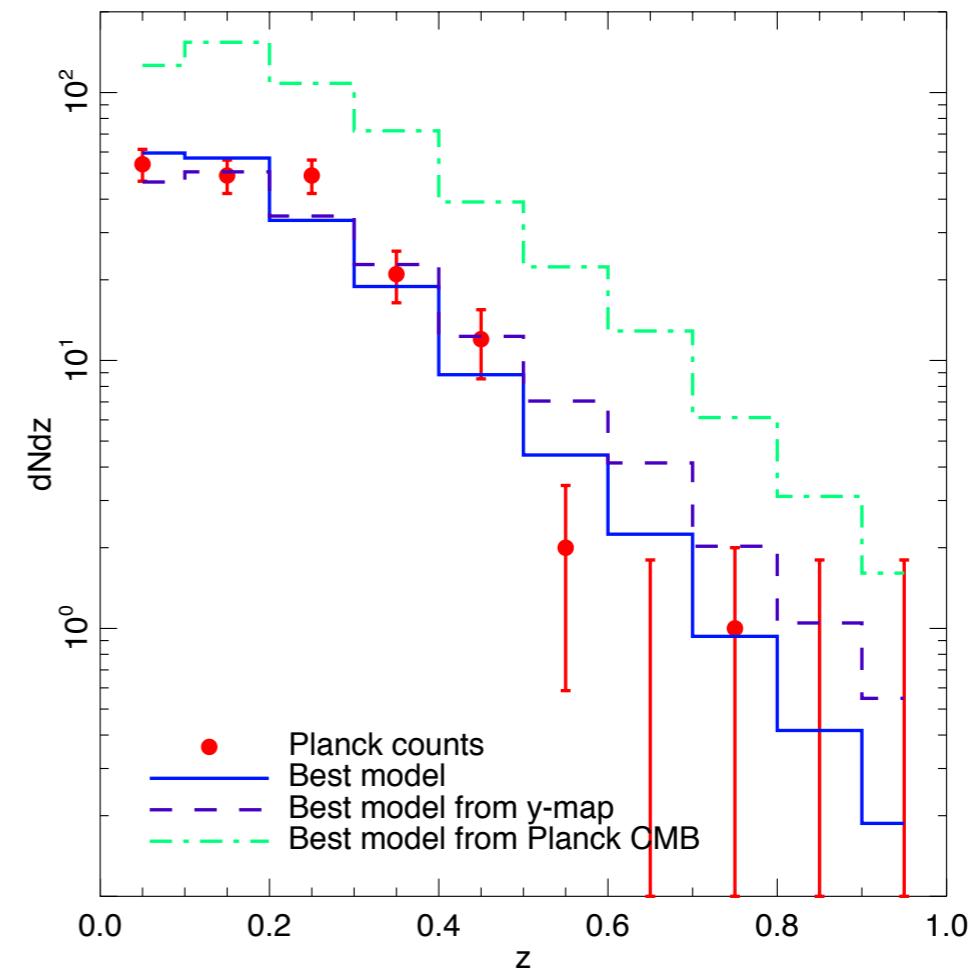
- shape of primordial power spectrum related to shape of inflaton potential (e.g. running $\Rightarrow V''$)
- small-scale $P(k)$ sensitive to physics of DM particles

Current best probe is Ly α forest (e.g. Seljak et al. 2006), but already approaching gas Jeans scale!

in future, CMB spectral distortions can probe $k \sim 10^4$

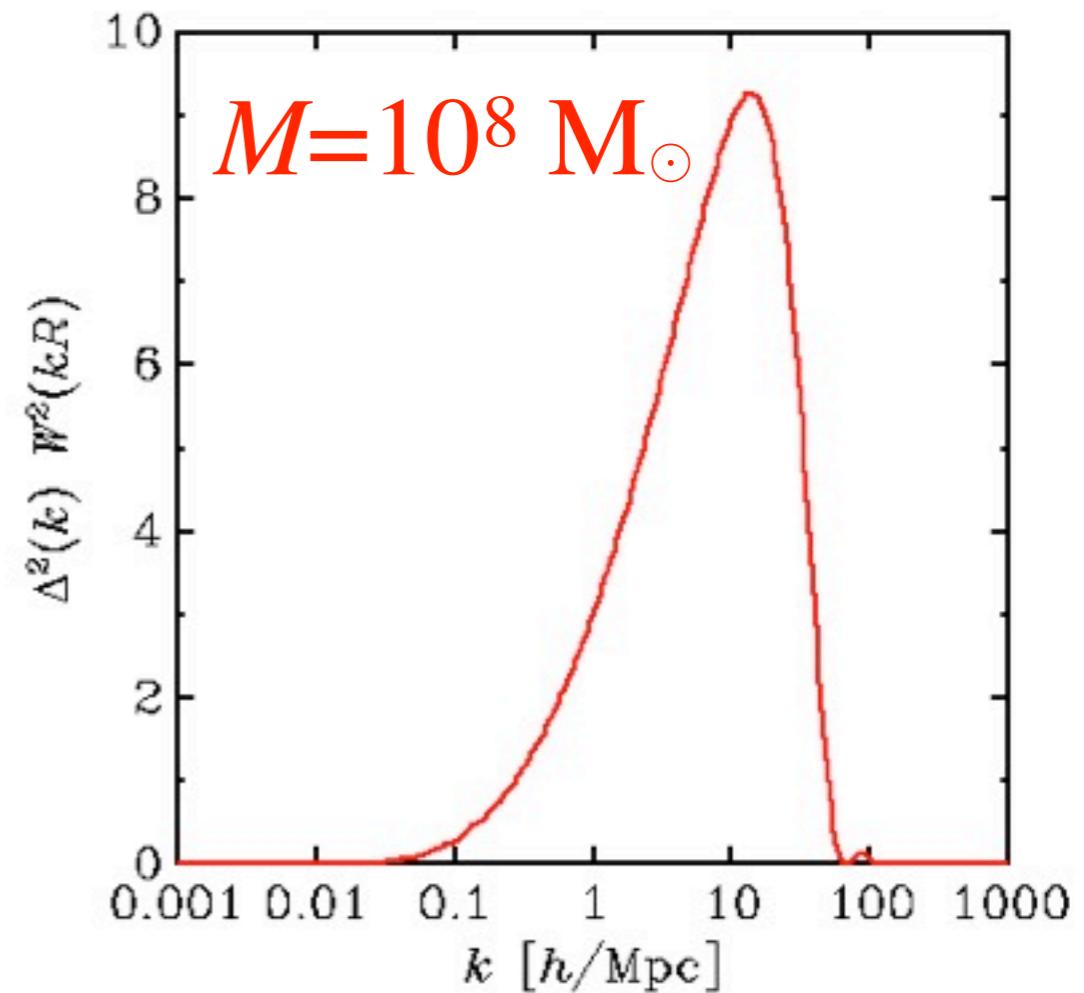
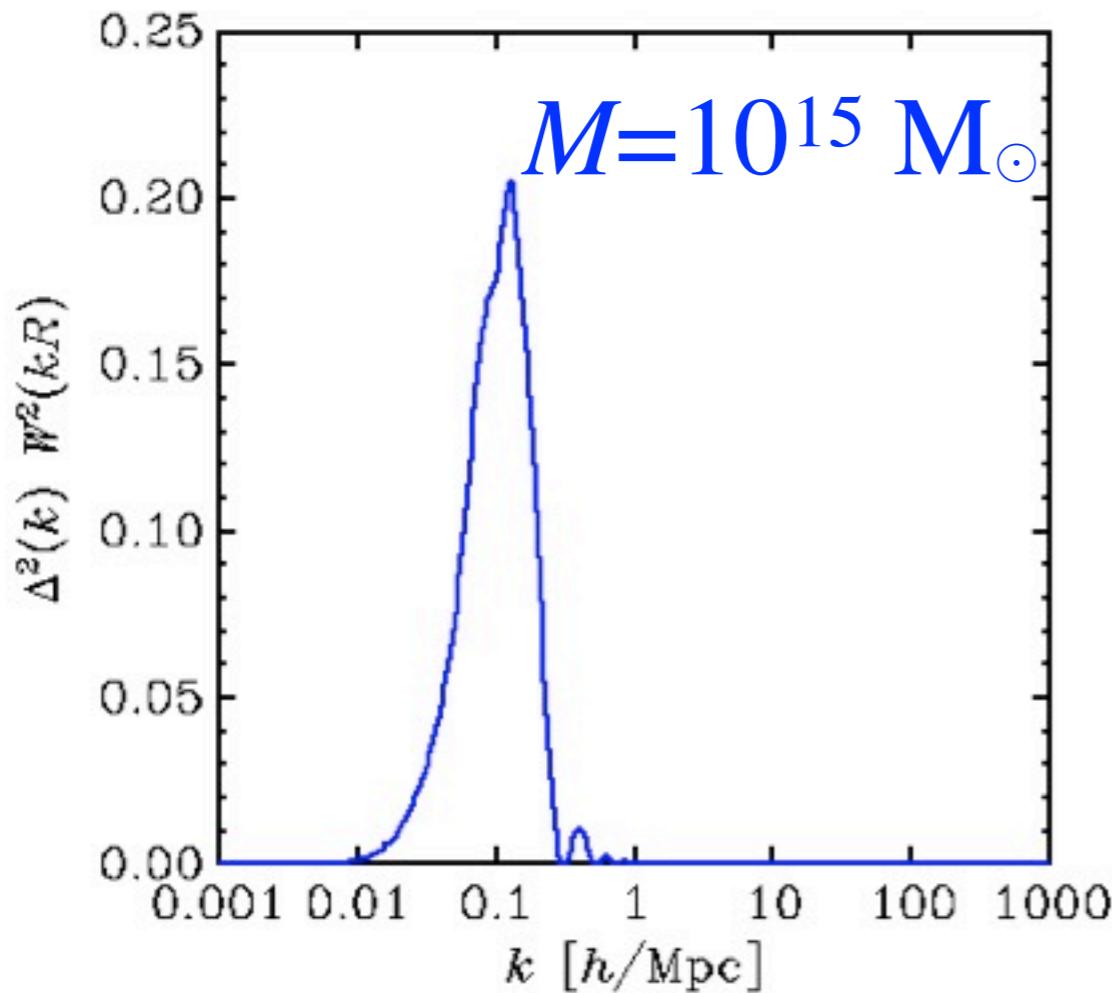
abundances

- abundance of objects (e.g. cluster dn/dM) is sensitive to power spectrum



abundances

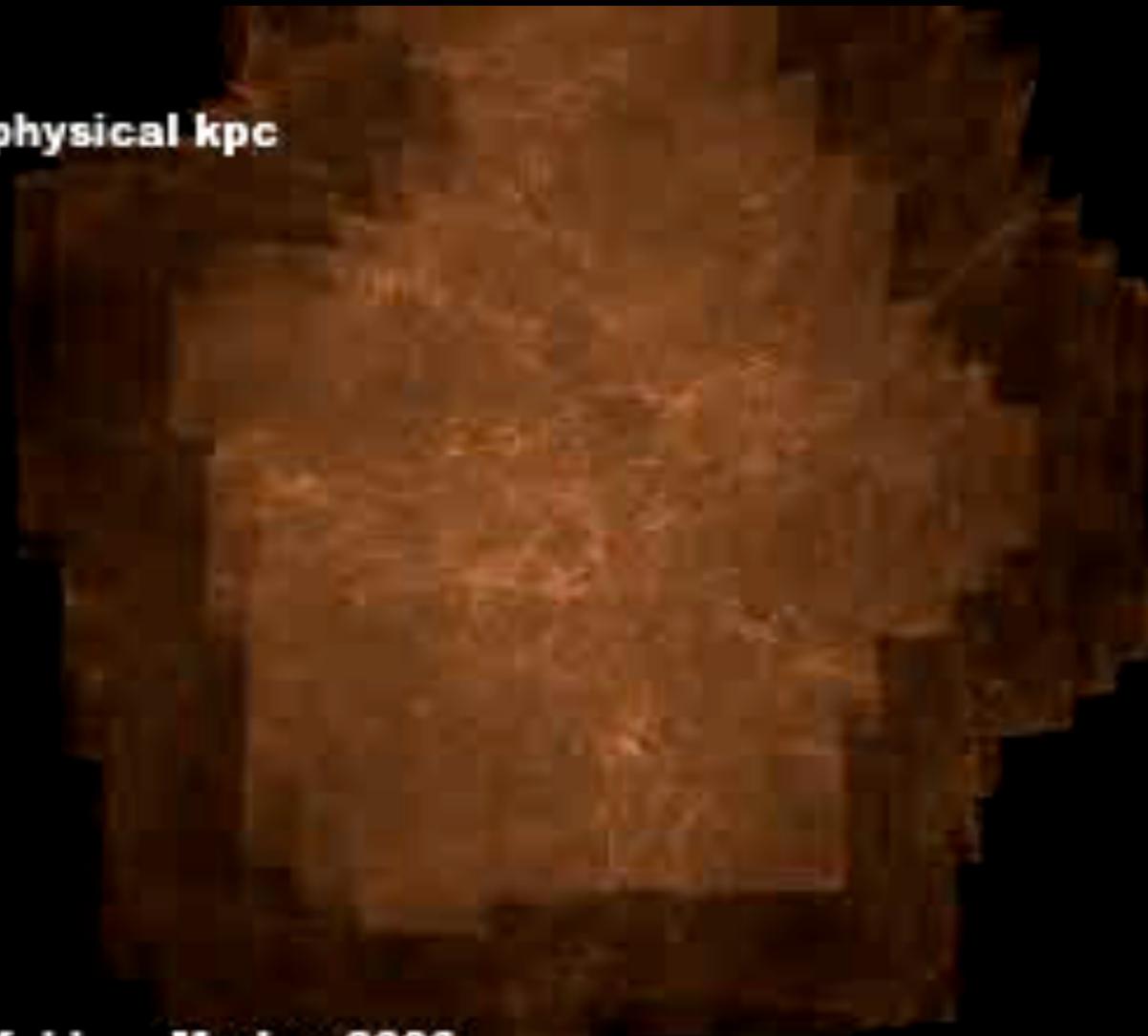
- abundance of objects (e.g. cluster dn/dM) is sensitive to power spectrum
- low mass halos & sub-halos sensitive to small-scale $P(k)$



halos and subhalos

$z=11.9$

800 x 600 physical kpc



“Via Lactea”
Diemand et al. 2006

Diemand, Kuhlen, Madau 2006

subhalos

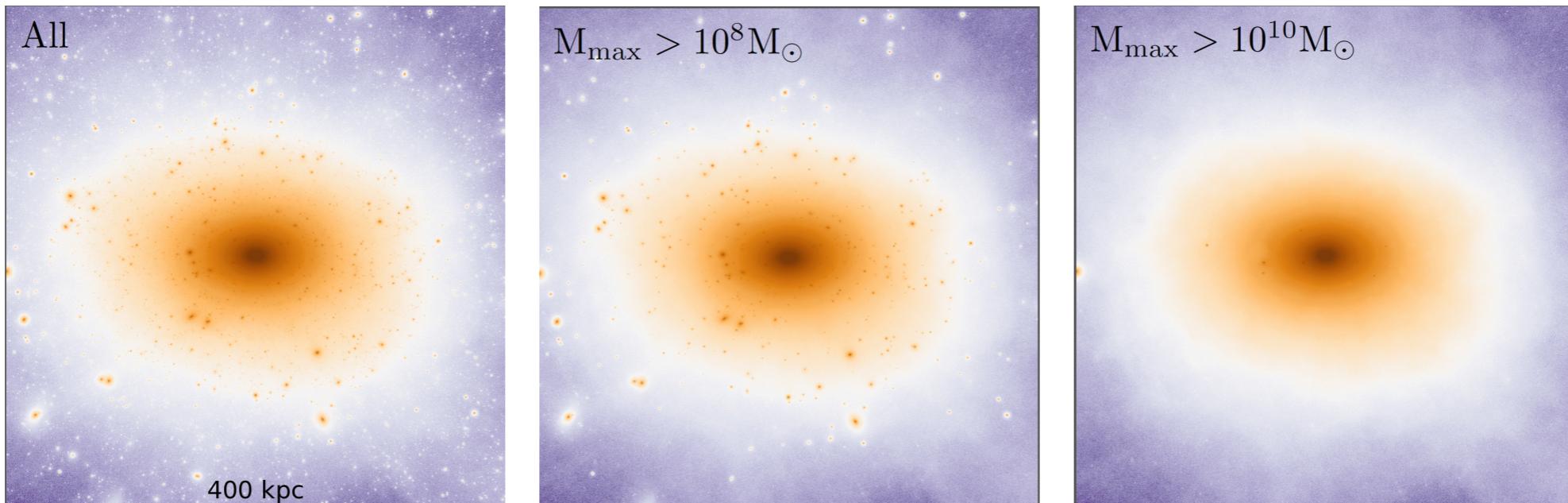
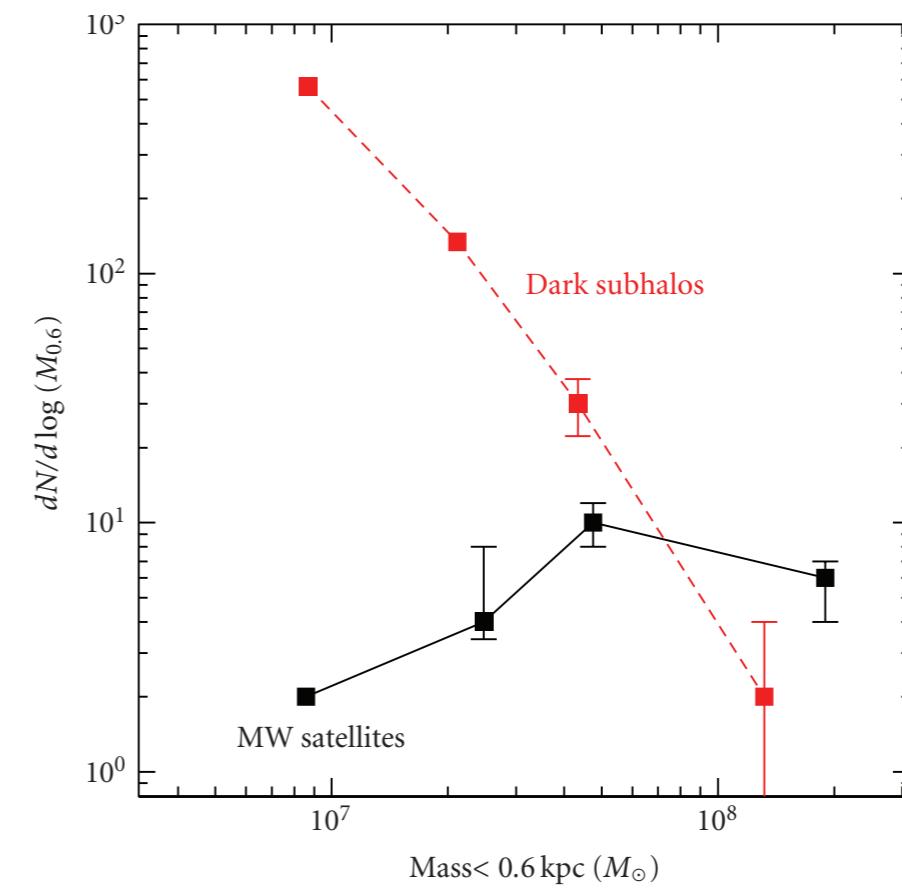
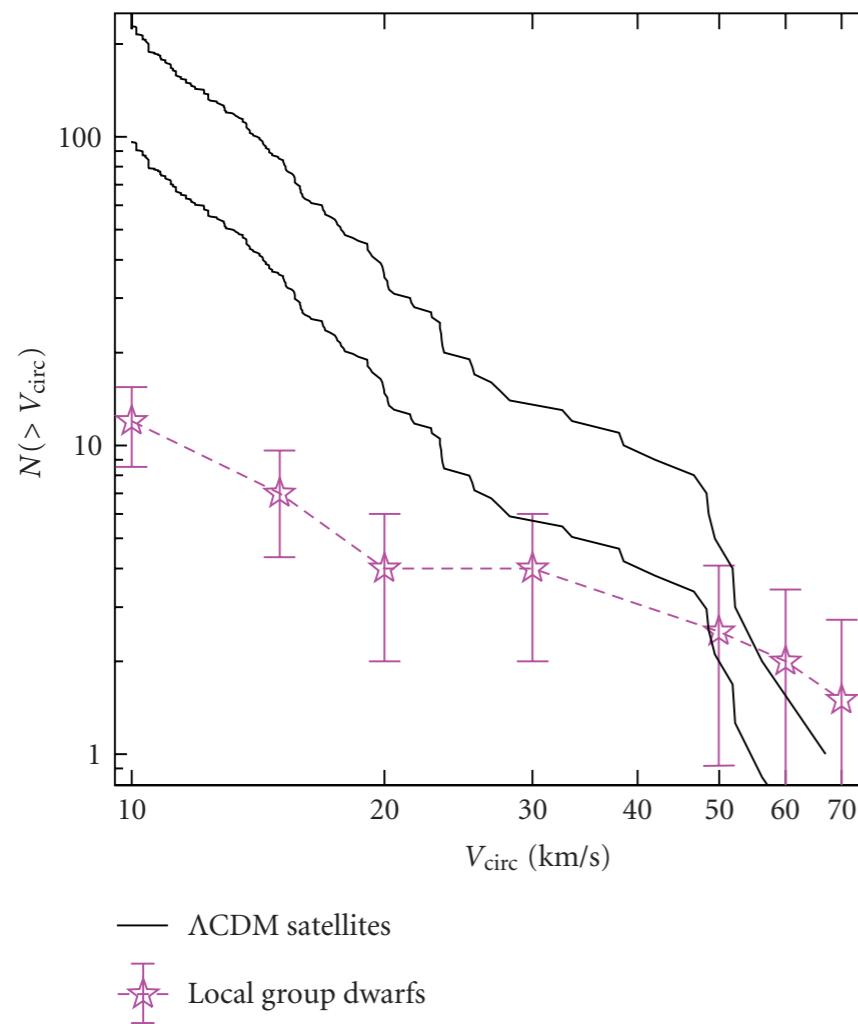


Figure 1: **Left:** Density projection in the Via Lactea-II simulation [18]. **Middle:** Similar, but excluding particles belonging to subhalos whose masses never exceeded $10^8 M_{\odot}$ any time throughout the simulation. **Right:** Like the middle panel, but excluding subhalos with $M_{\max} < 10^{10} M_{\odot}$. This sequence should qualitatively illustrate the effect of truncating the power spectrum on substructure content in DM halos.

How to measure?

- count small galaxies / satellites
- ➡ missing satellite problem (see Kravtsov 2012 for recent review)



How to measure?

- count small galaxies / satellites
 - ➡ missing satellite problem (see Kravtsov 2012 for recent review)
 - ➡ but low-mass subhalos could be dark...
- need *gravitational* probe to see dark halos/subhalos
 - heating of tidal streams (e.g. Carlberg 2012)
 - gravitational lensing!

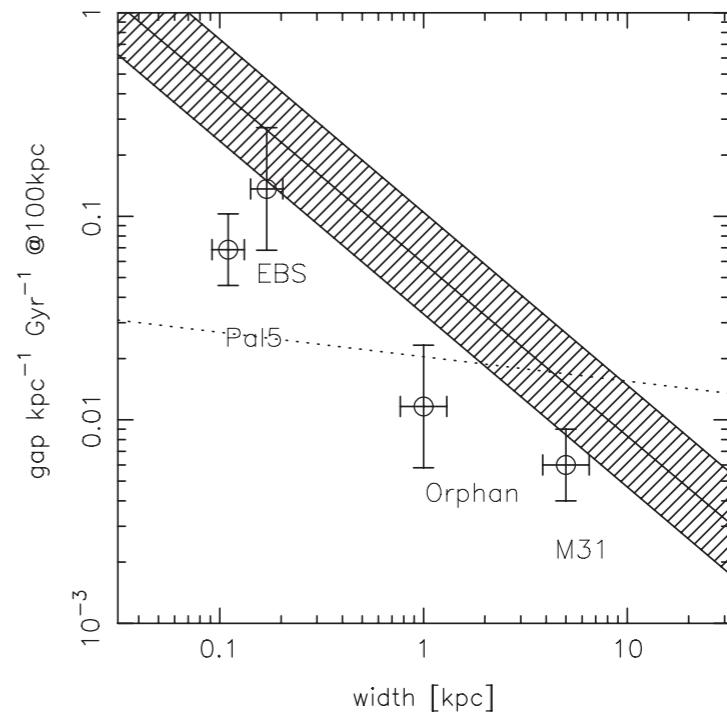
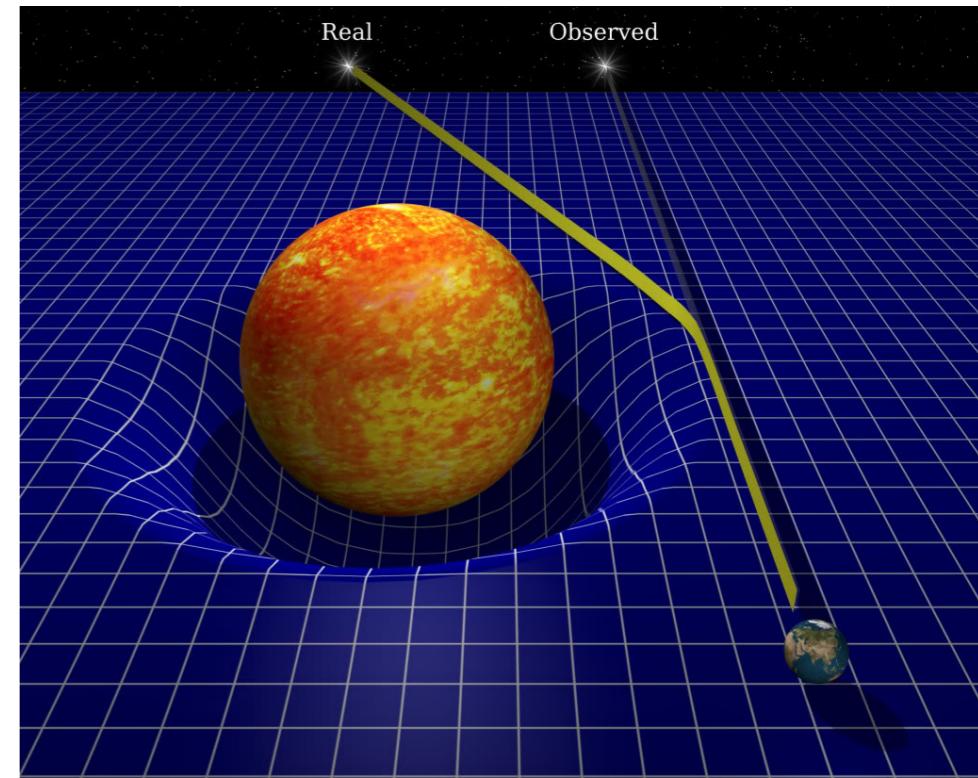


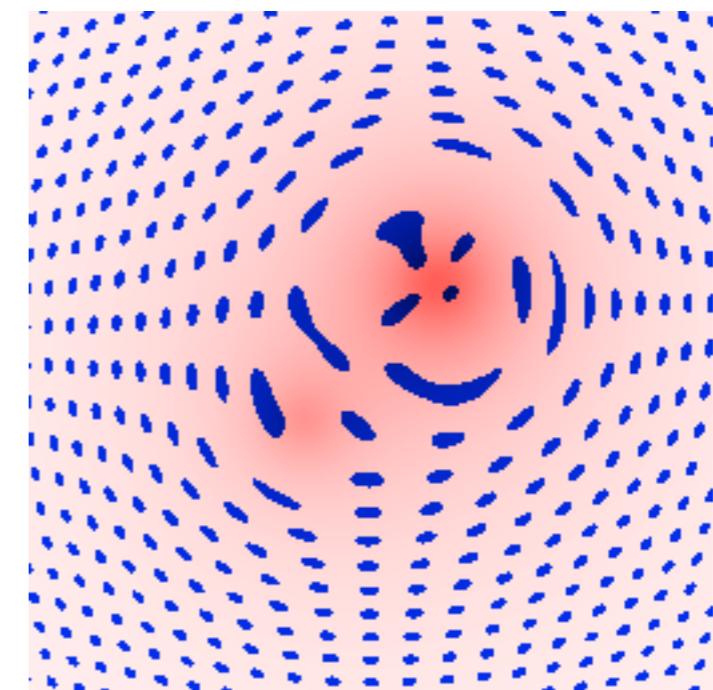
Figure 11. Estimated gap rate vs. stream width relation for M31 NW, Pal 5, the EBS, and the CDM halo prediction. All data are normalized to 100 kpc. The width of the theoretical relation is evaluated from the dispersion in the length-height relation of Figure 8. Predictions for an arbitrary alternative mass functions, $N(M) \propto M^{-1.6}$, normalized to have 33 halos above $10^9 M_\odot$ are shown with a dotted line.

Gravitational lensing

- the deflection of light rays caused by inhomogeneities
- also distorts the apparent shapes & sizes of observed sources
- amount of lensing characterized by convergence $\kappa \sim \int \delta\rho \, dl$
- Two regimes:
 - ◆ **weak lensing** ($|\kappa| \ll 1$) : small distortion
 - ◆ **strong lensing** ($\kappa \gtrsim 1$) : large distortion & multiple imaging



credit:
D. Jarvis



credit:
E. Wright

subhalo lensing

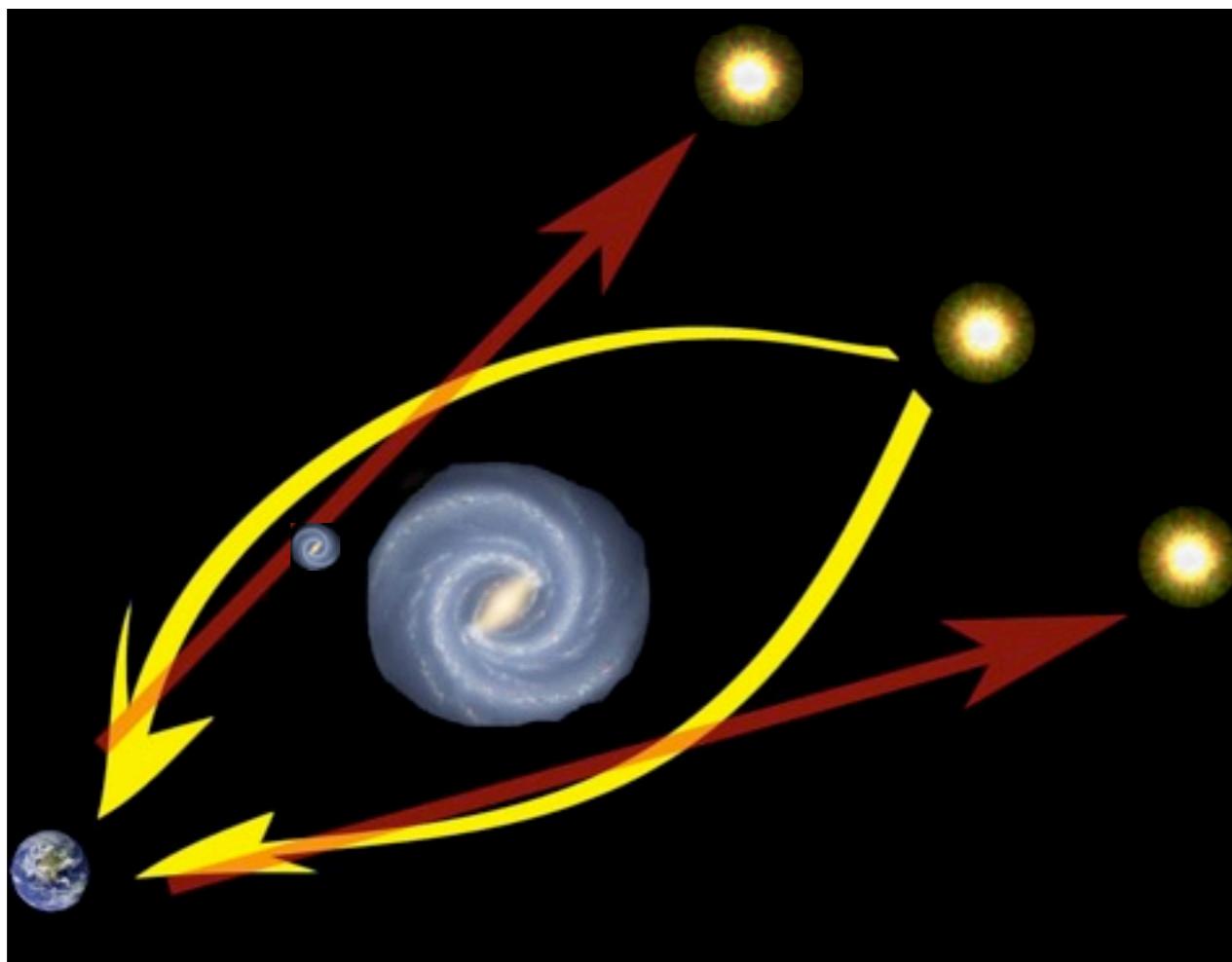
small ($M < 10^8 M_\odot$) halos and subhalos are wimpy lenses!

- small size ($\lesssim \text{kpc}$), so each one affects a small fraction of the sky
- lensing amplitude is weak (central $\kappa, \gamma \lesssim 0.1$)
- can't stack if they're dark (where to stack?)
- need a way to boost their effect to detect them...

strong lensing



- if a small halo/subhalo projects near a **strong lens**, then the big lens can magnify the lensing effect of the small halo

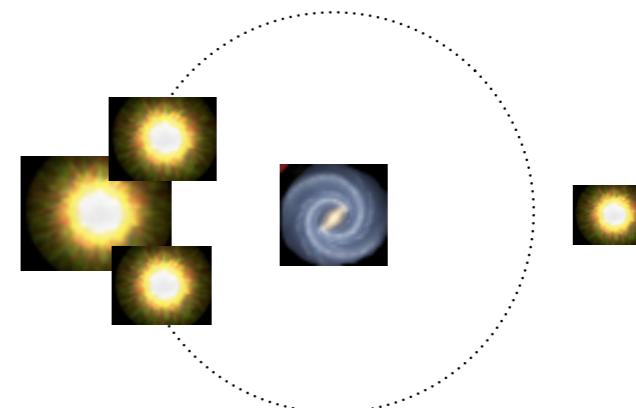
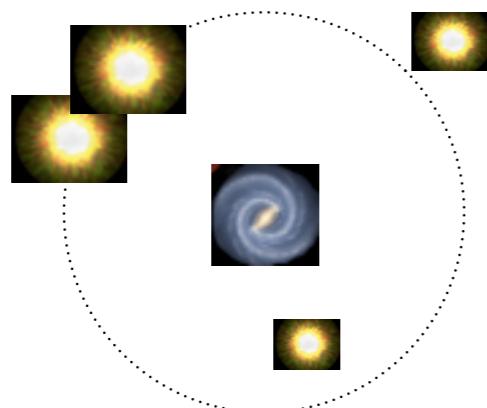


$$\Delta\theta \approx M \cdot \Delta\alpha$$

if high magnification,
then perturbation
can have big effect!
(Mao & Schneider 1998)

universality relations

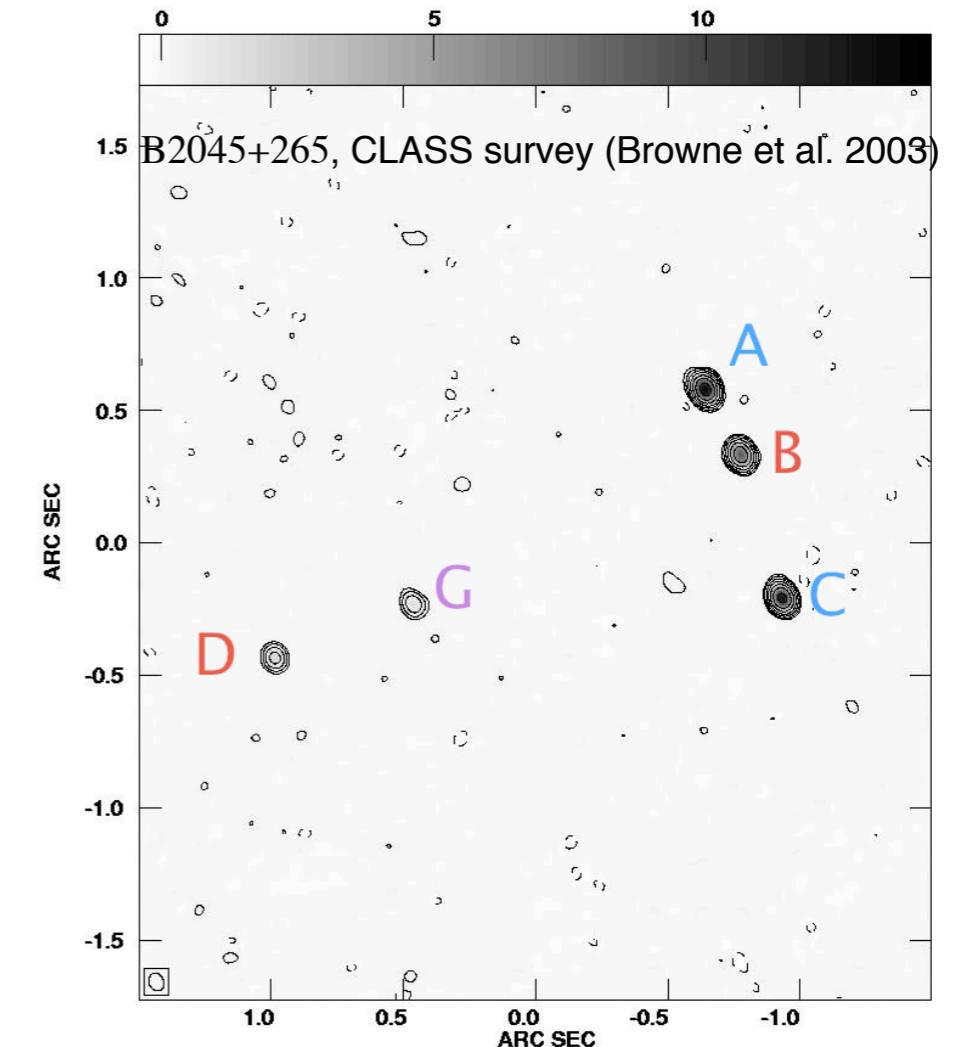
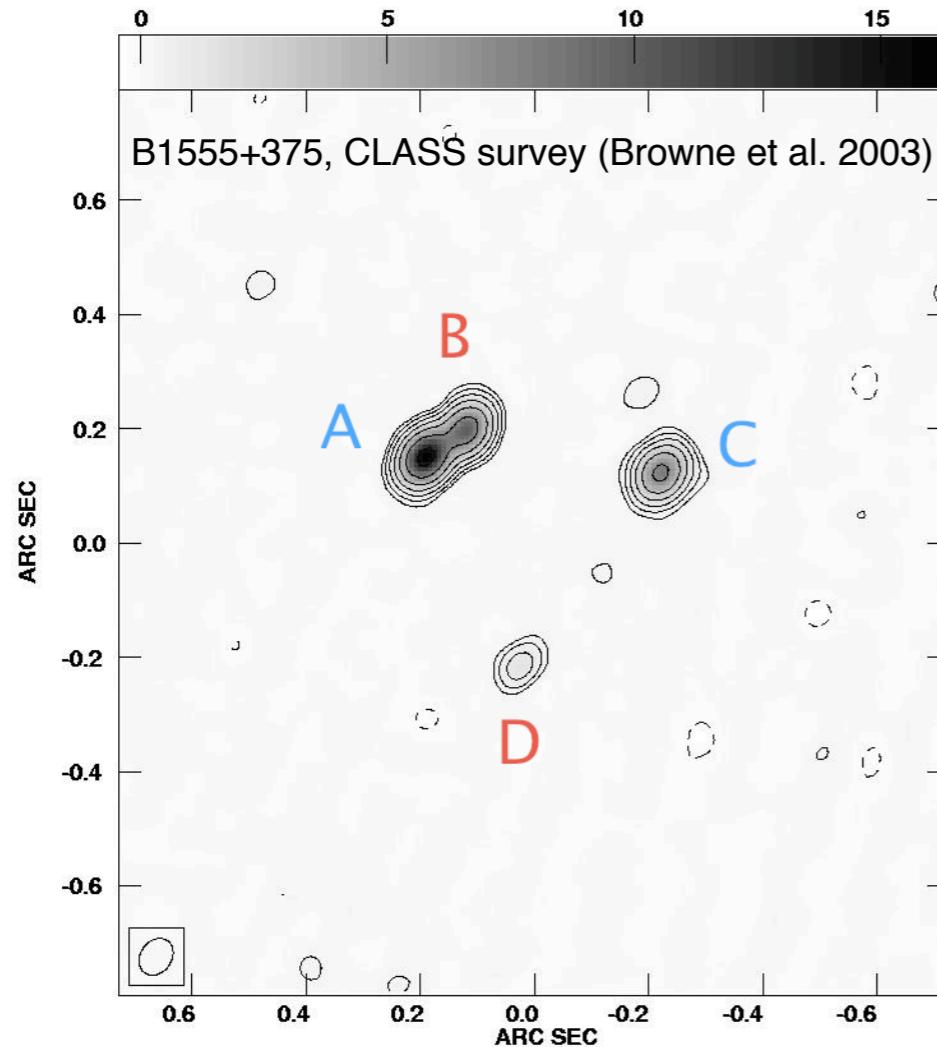
- when 2 images are close together, they *should* have nearly equal brightness
- similar relation when 3 images occur close together:



$$\frac{\Delta f}{f} \propto \frac{\Delta r}{r_s}$$

$$\frac{f_A - f_B + f_C}{f_A + f_B + f_C} \propto \frac{\Delta r}{r_s}$$

universality relations



$$\frac{\Delta f}{f} \propto \frac{\Delta r}{r_s}$$

$$\frac{f_A - f_B + f_C}{f_A + f_B + f_C} \propto \frac{\Delta r}{r_s}$$

flux anomalies

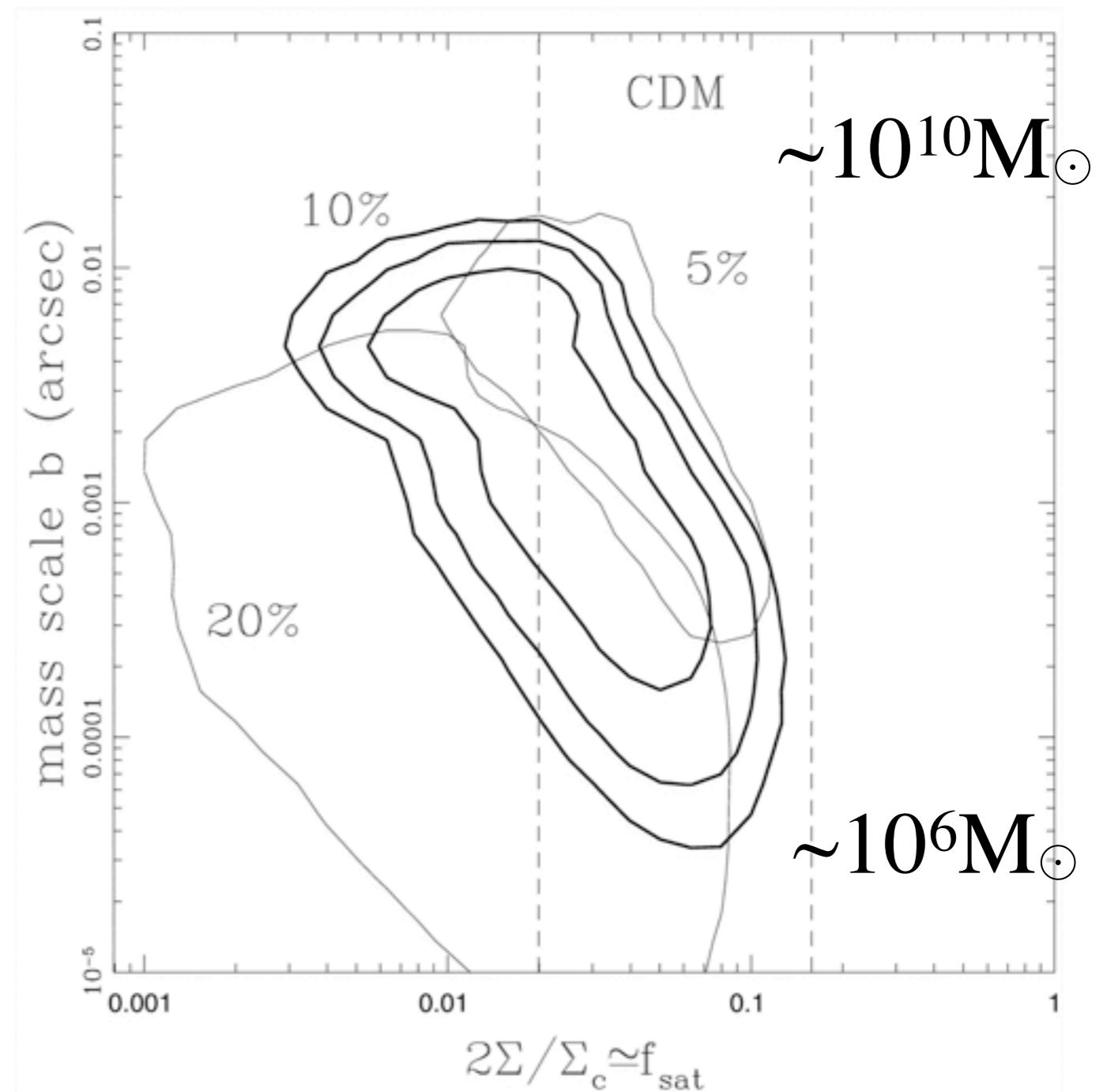
- implication: local scale length r_s is much smaller than size of the system \Rightarrow **substructure** in the potential
- in radio quasars, flux ratio anomalies can only be caused by mass substructure (not true for optical lenses)
- flux anomalies occur in almost all of the observed quasar lenses \Rightarrow lots of substructure!

how do we know it's substructure?

- radio flux ratios independent of λ , as expected for lensing but unlike propagation effects (like scintillation or dust extinction)
- observed **parity** dependence:
 - + parity magnified, – parity demagnified
- radio quasars too big to be affected by stellar microlensing, unlike stellar QSO's.
- see Kochanek & Dalal (2003) for more...

analysis of radio lenses

- Dalal & Kochanek (2002) analyzed sample of **7** radio lenses
- found that $\sim 1\%$ of projected mass at 5kpc is in substructure
- but uncertainty was about factor of 10!

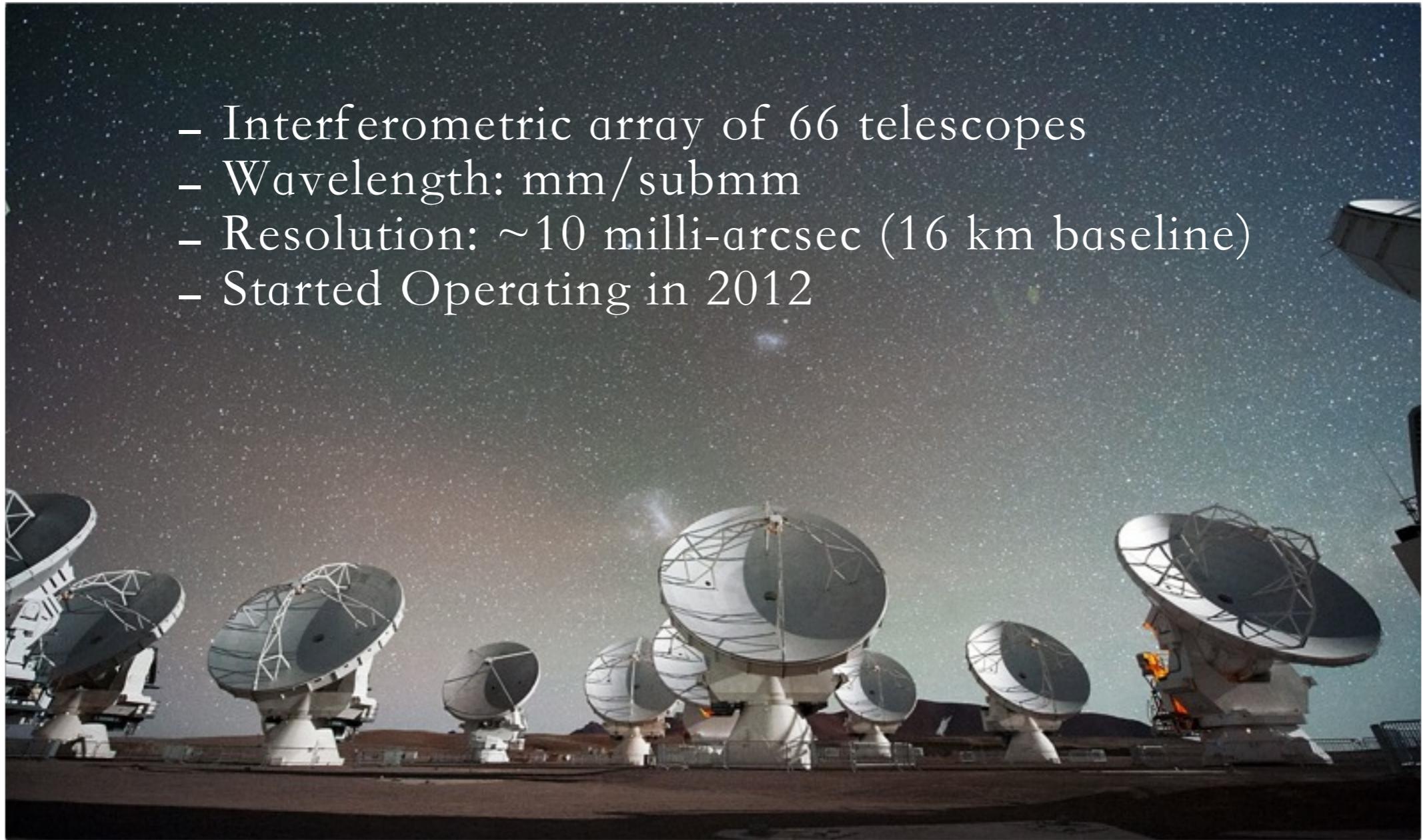


how to improve?

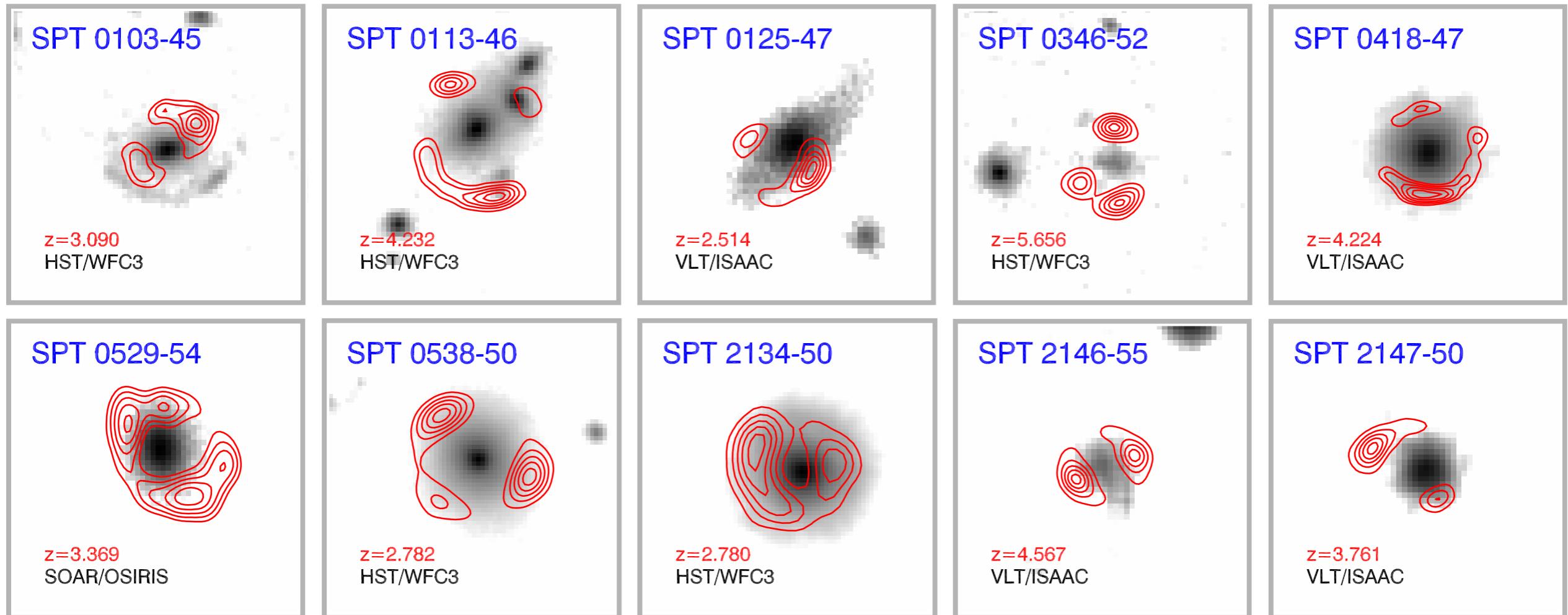
- we need a new class of lensed sources!

ALMA

- Interferometric array of 66 telescopes
- Wavelength: mm/submm
- Resolution: \sim 10 milli-arcsec (16 km baseline)
- Started Operating in 2012



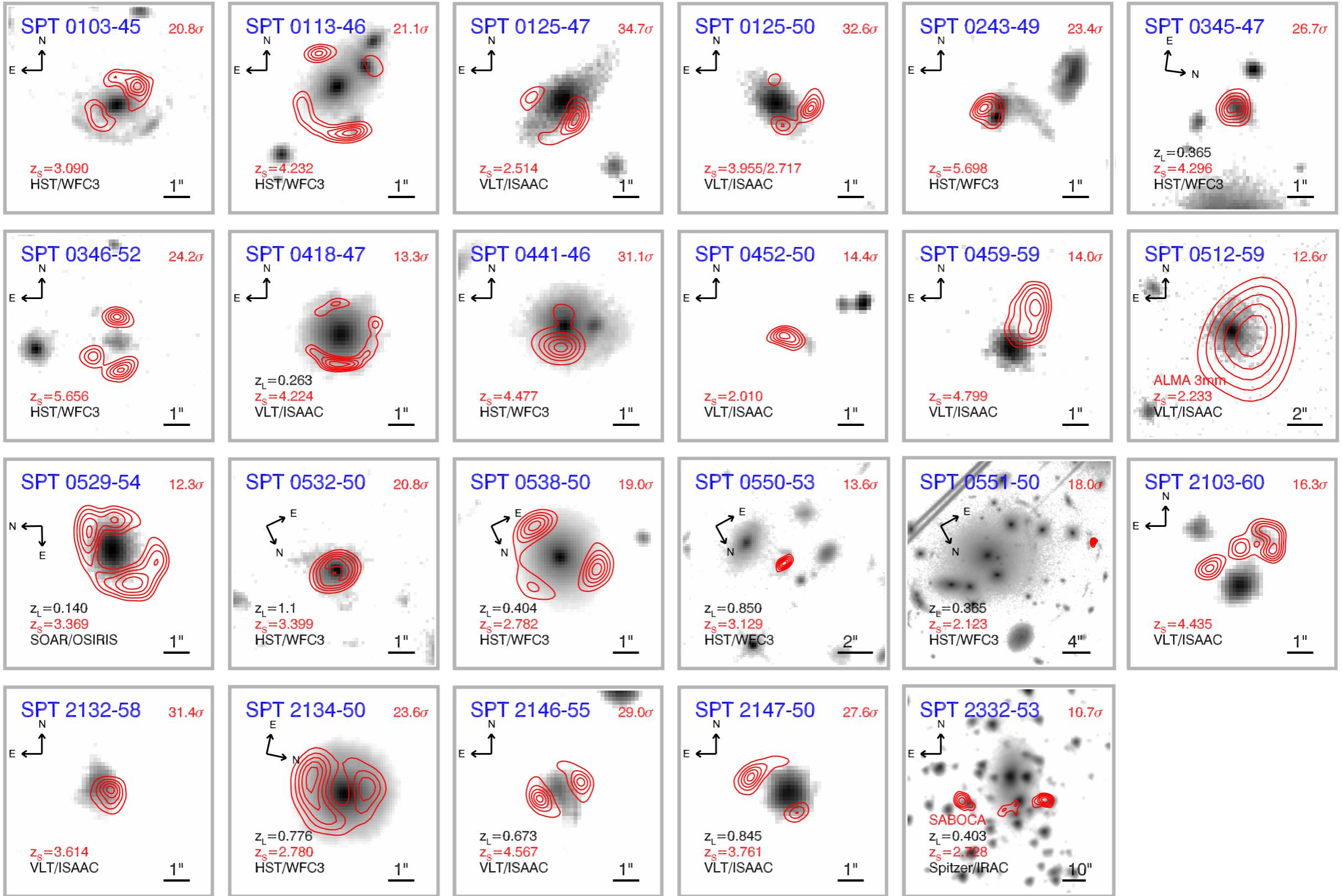
ALMA Cycle 0 Band 7 350 GHz 2 minute snapshots



8" x 8" boxes

- = deep NIR imaging
- = 2 minute ALMA 350 GHz snapshot

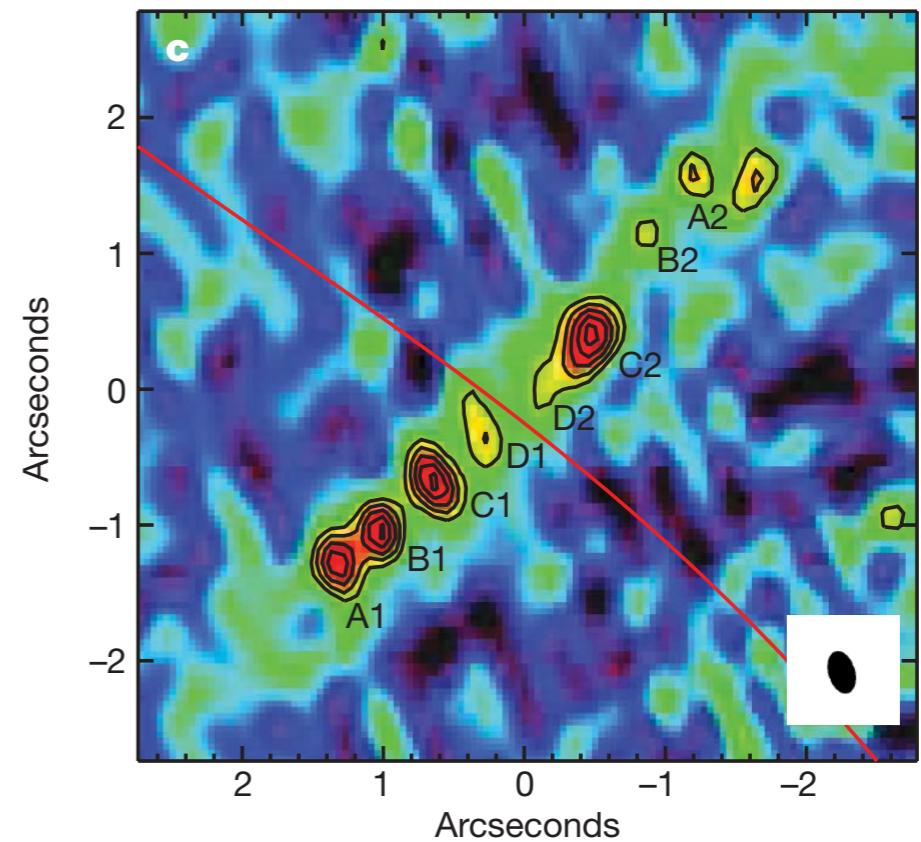
Note that sources are bright in submm and invisible in visible/IR,
while lenses are invisible in submm and bright in visible/IR.



= NIR imaging
= submm imaging

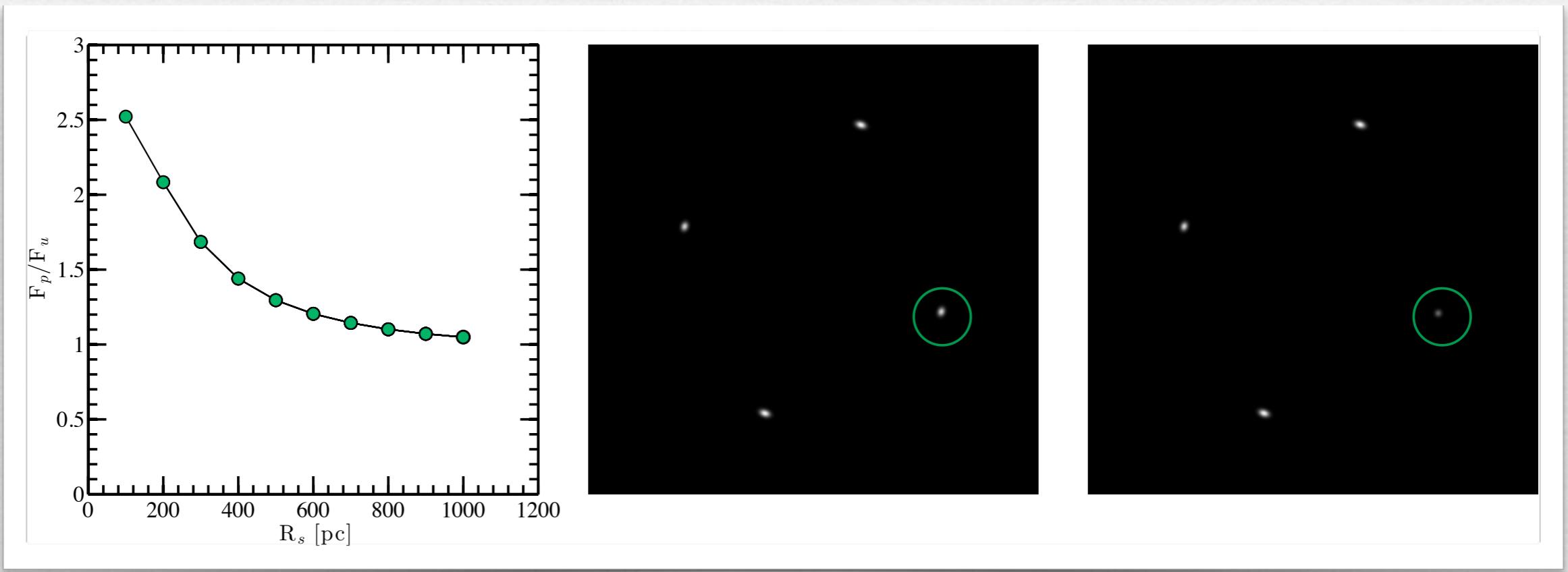
okay.... so what?

- lensed SMG's are *perfect* for detecting substructure!
- theoretically, we expect these galaxies to contain many **compact** star-forming clumps ($\sim 100\text{pc}$) inside much bigger GMC's ($\sim \text{kpc}$). see also local analogues like Arp 220
- clumps are extremely bright in lines like CO 7-6
- example: high resolution SMA imaging of lensed SMG reveals compact source clumps (Swinbank et al. 2010)

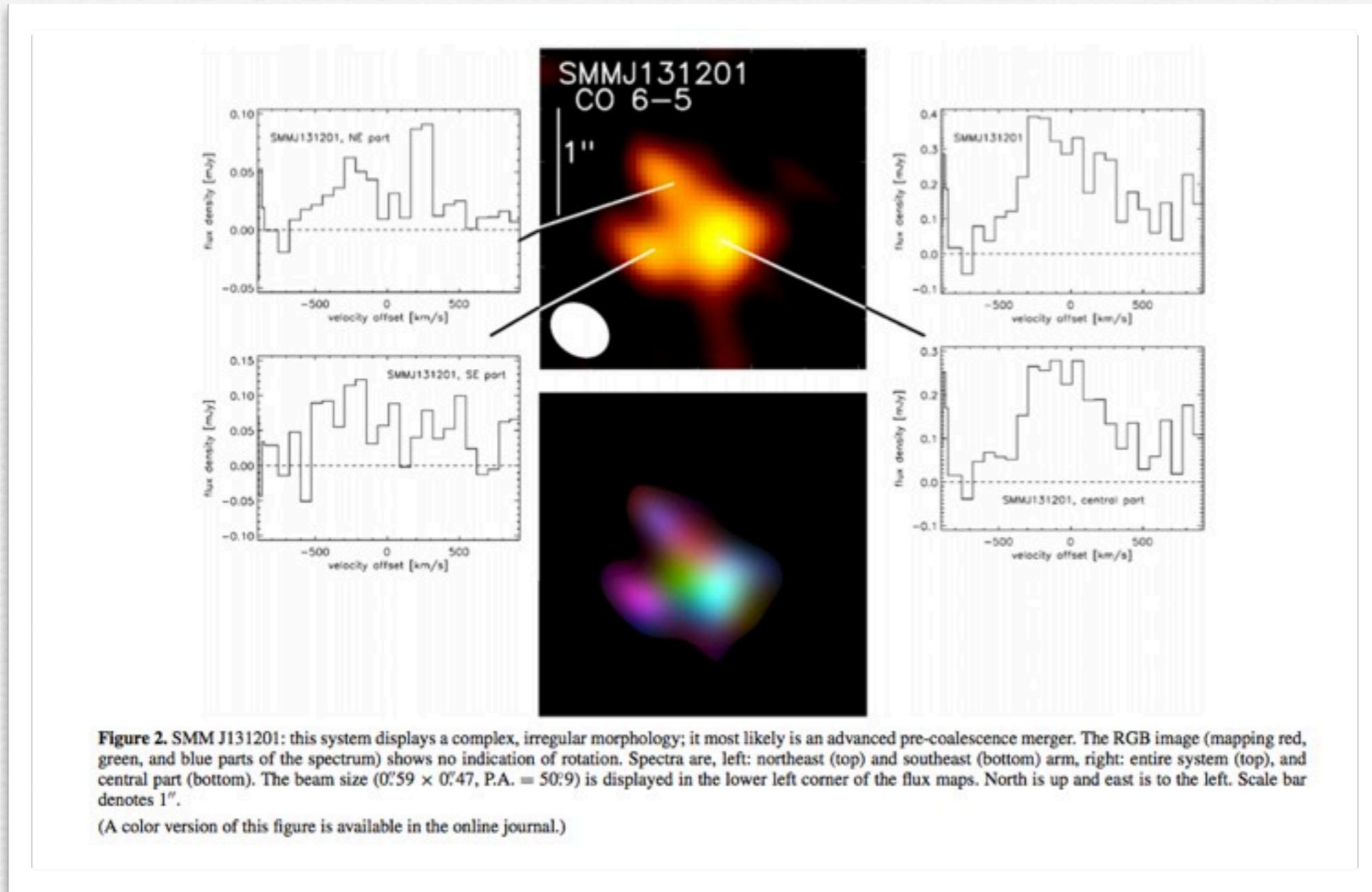


The Strength of Substructure Lensing Signal Depends on the Source Size

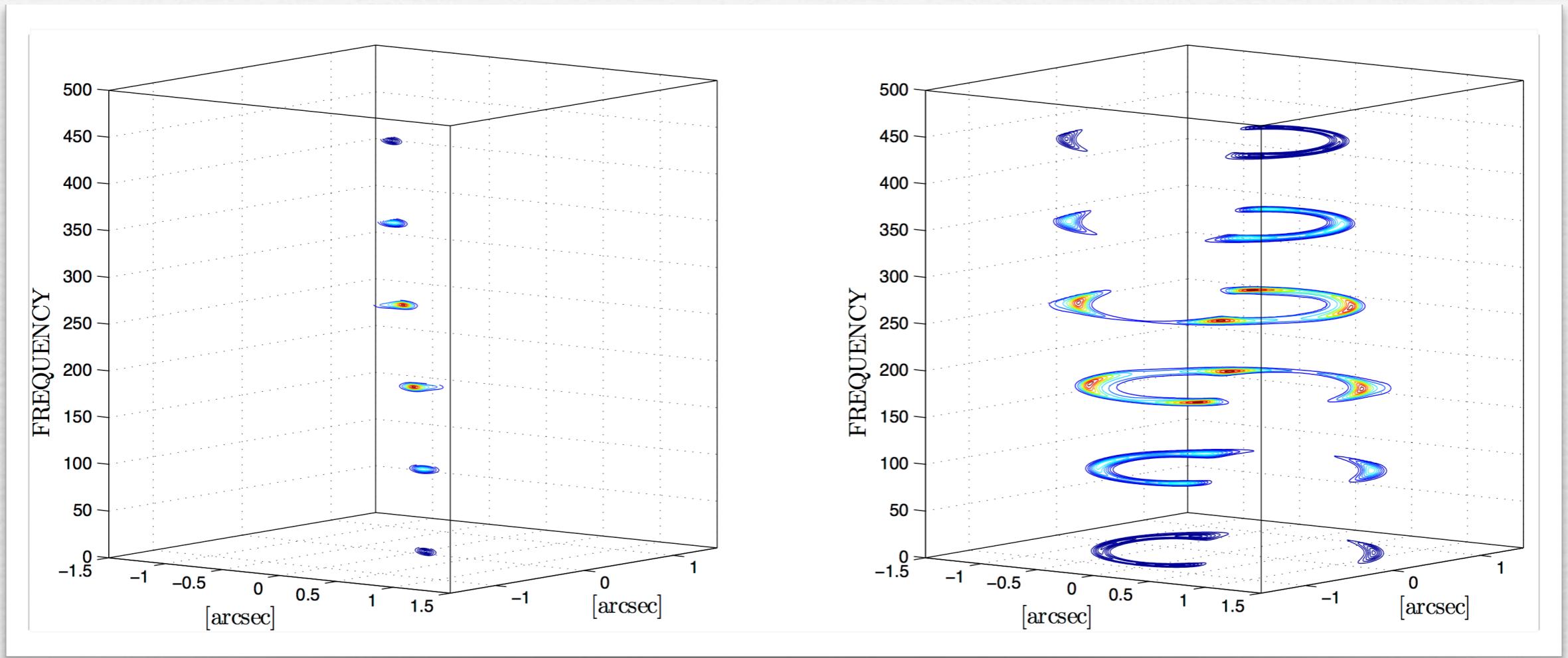
Compact Sources Are Perturbed More Strongly



Spatially resolved spectroscopy



Velocity decomposition can separate small features of the source



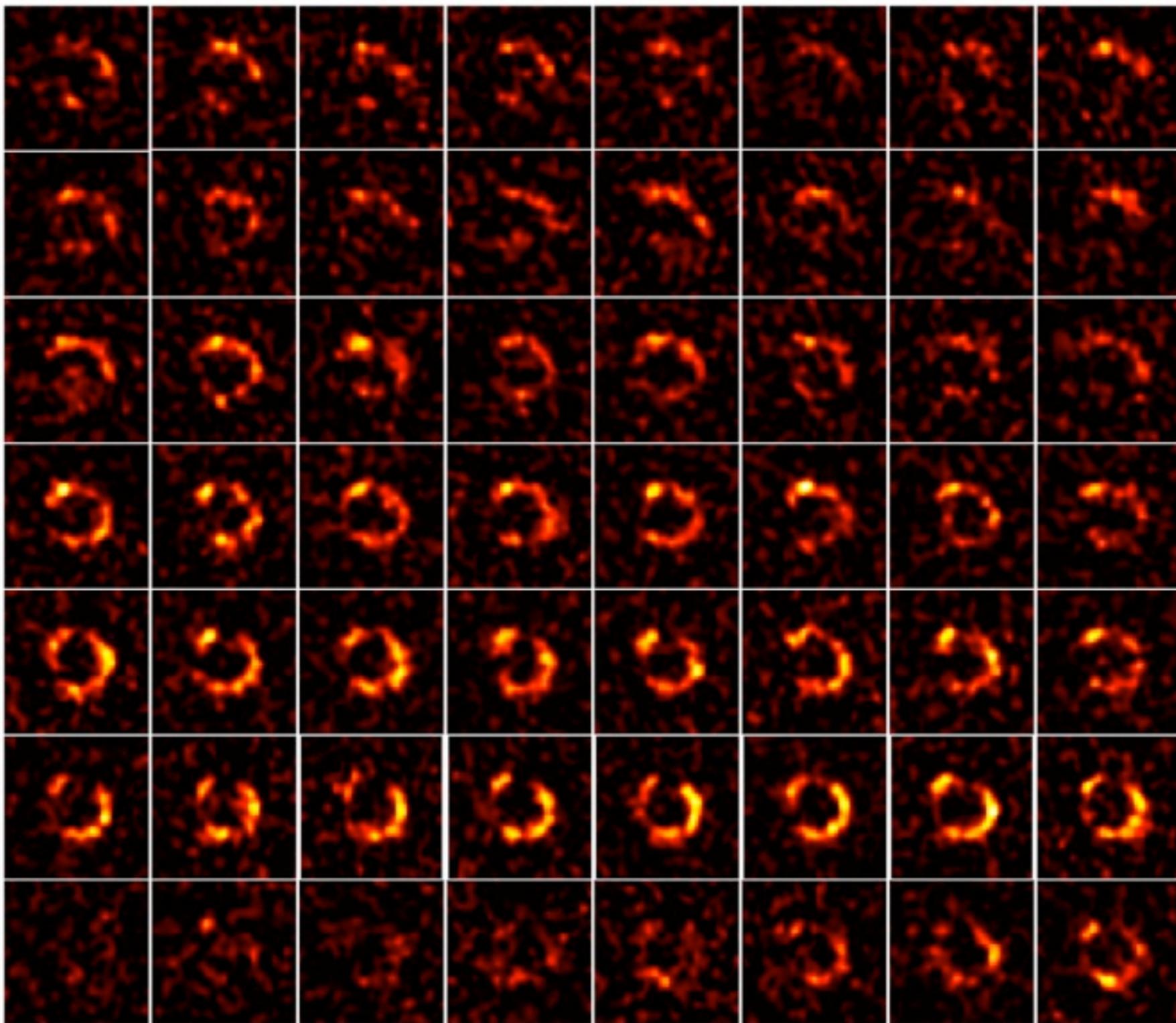
so each SMG is equivalent to having
many sources behind each lens!

Preliminary results

Our first observations were taken late last year;
here are some early results...



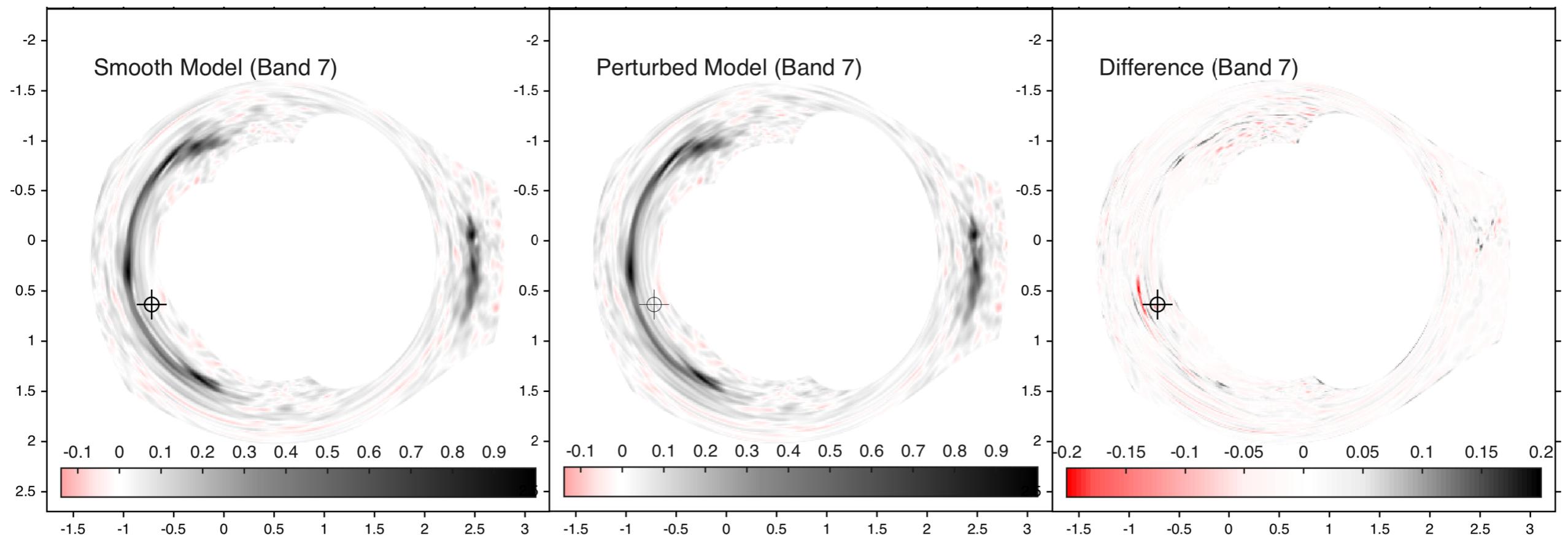
3D structure



Lens modeling

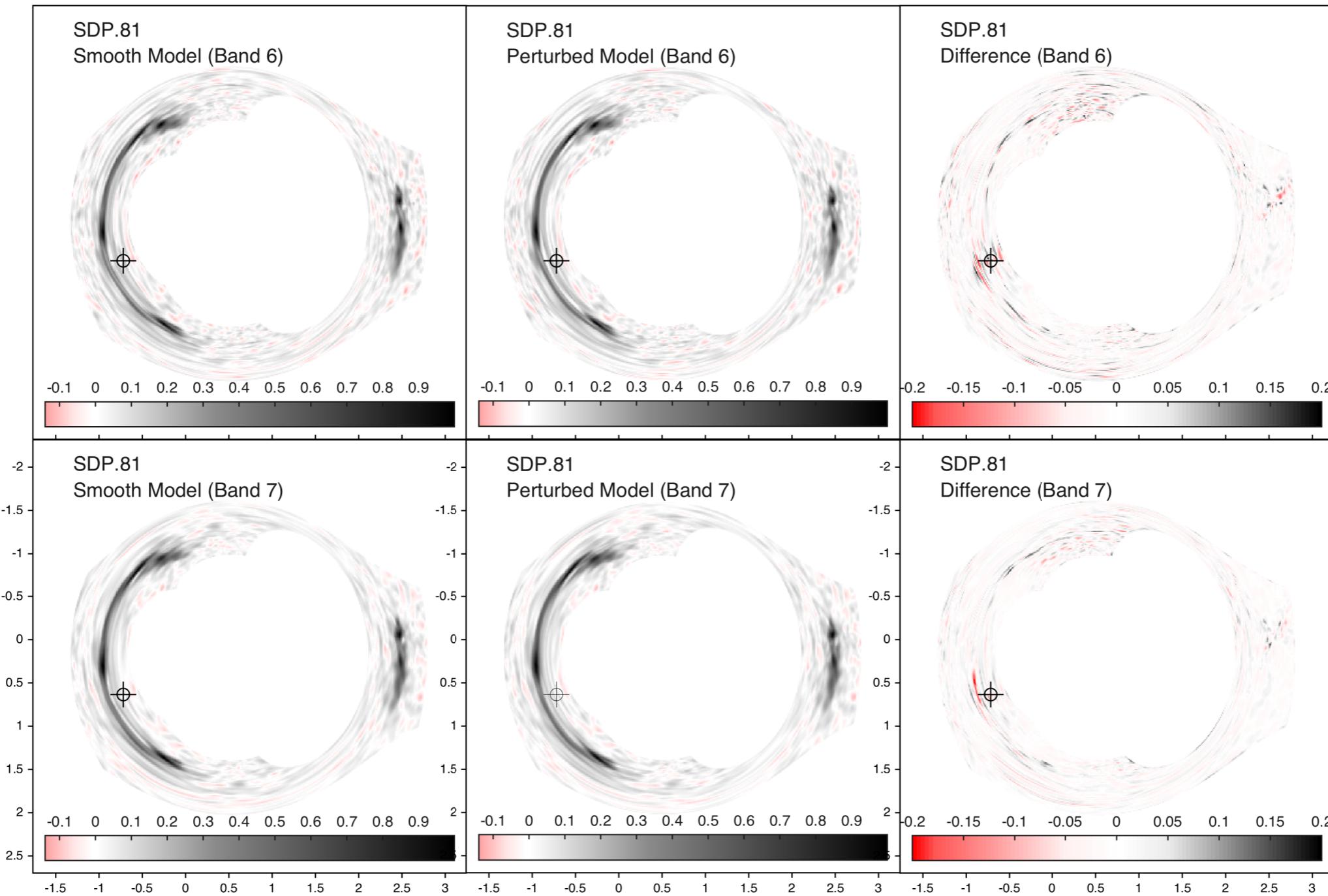
- ALMA is an interferometer, so the observables are (millions of) visibilities in the uv plane
- We fit the visibilities, not CLEAN images
- Our model has 10's of thousands of free parameters, including things like time-varying antenna phase errors. We marginalize over all of them.
- This is crucial! Improper treatment of phase errors will lead to spurious detection of subhalos

Subhalo detection

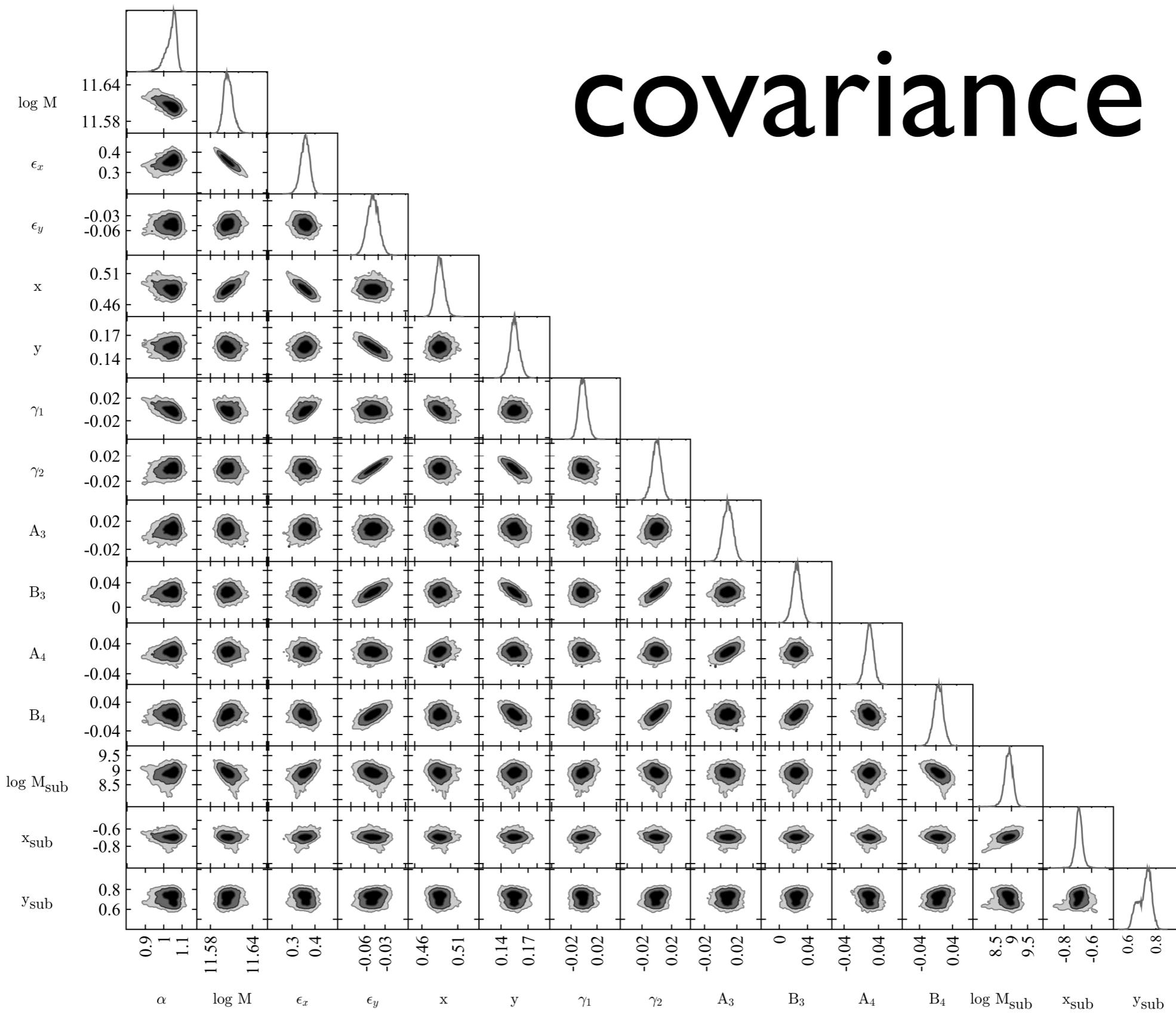


- a $M=10^9 M_\odot$ subhalo is detected at ~ 7 -sigma confidence in the first system we analyzed

detected in multiple bands

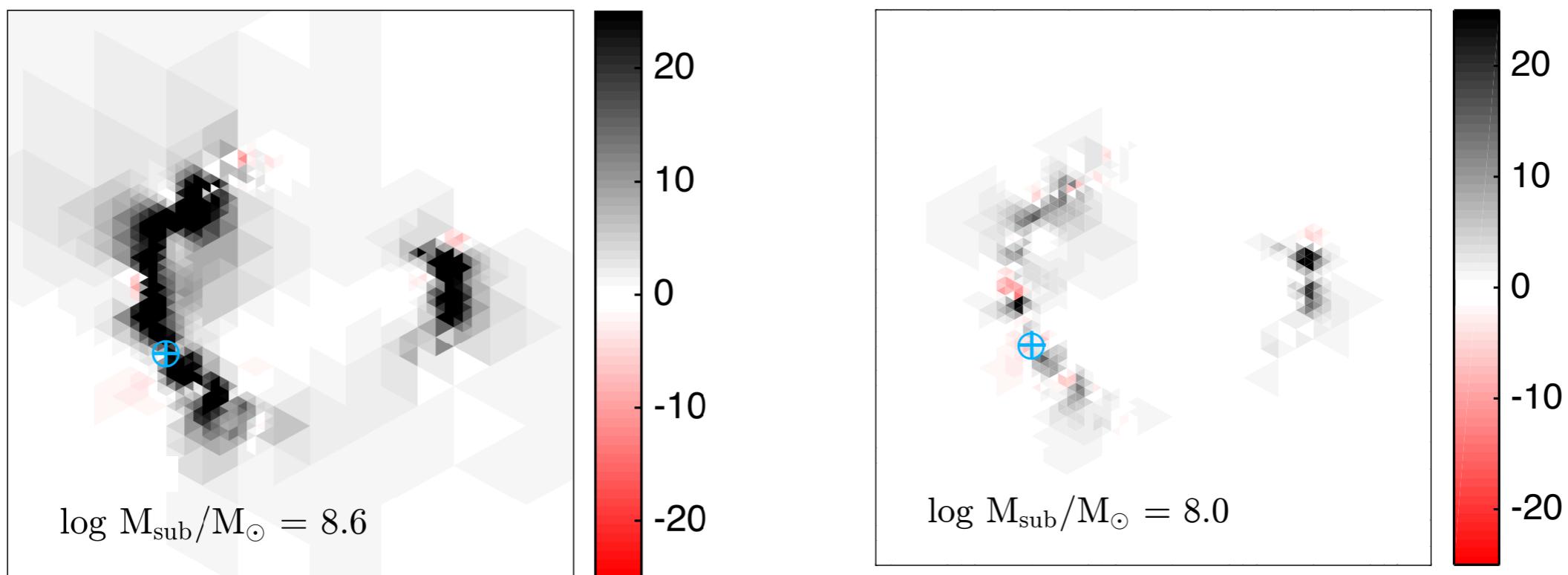


covariance



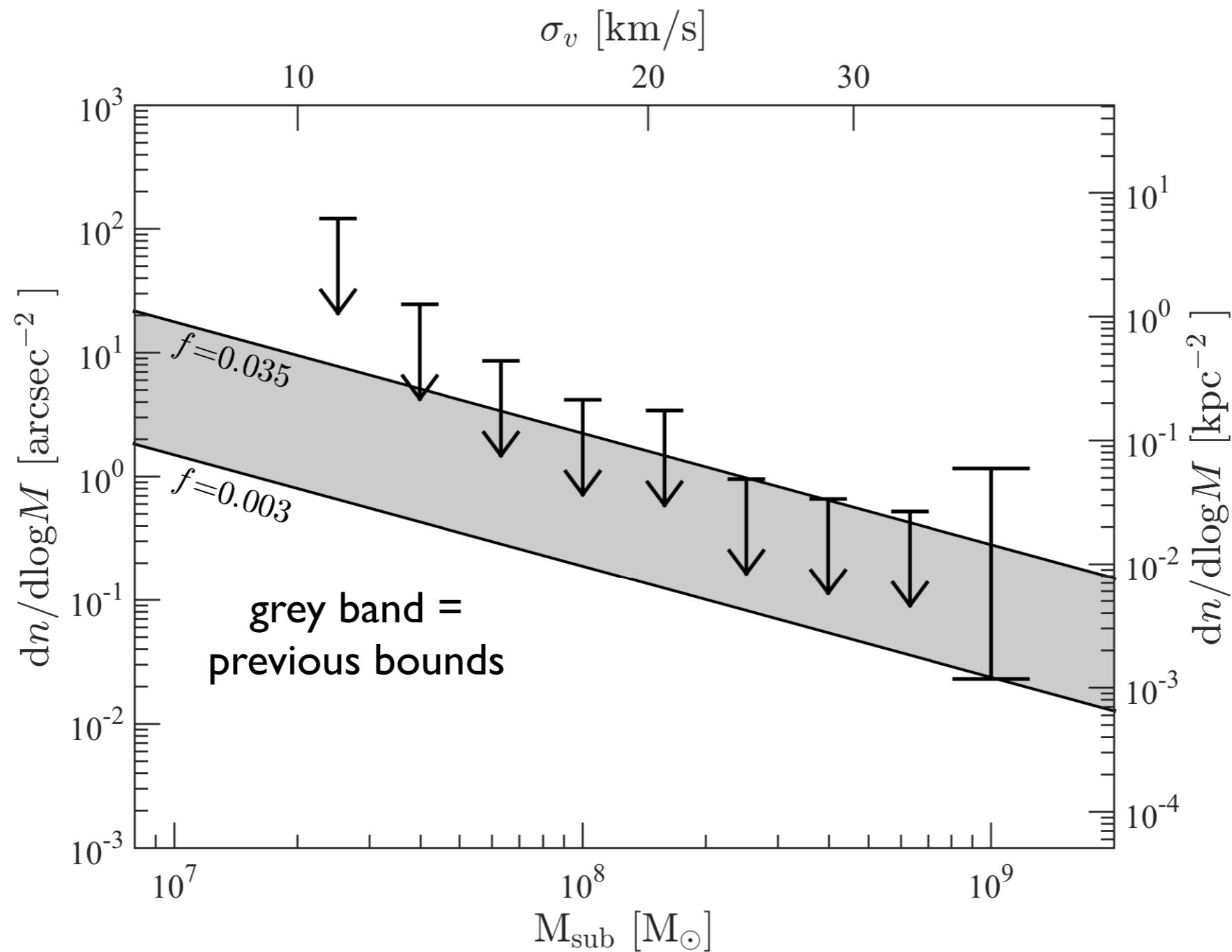
Other subhalos?

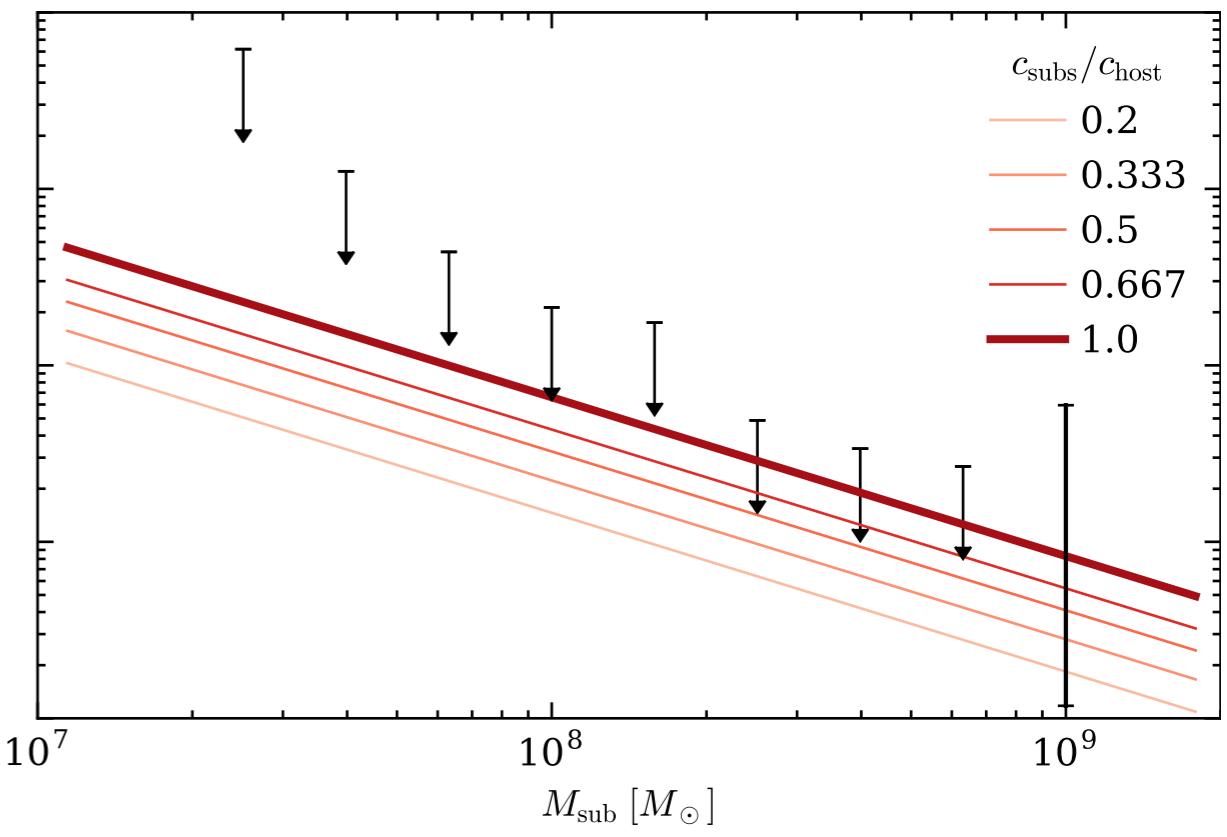
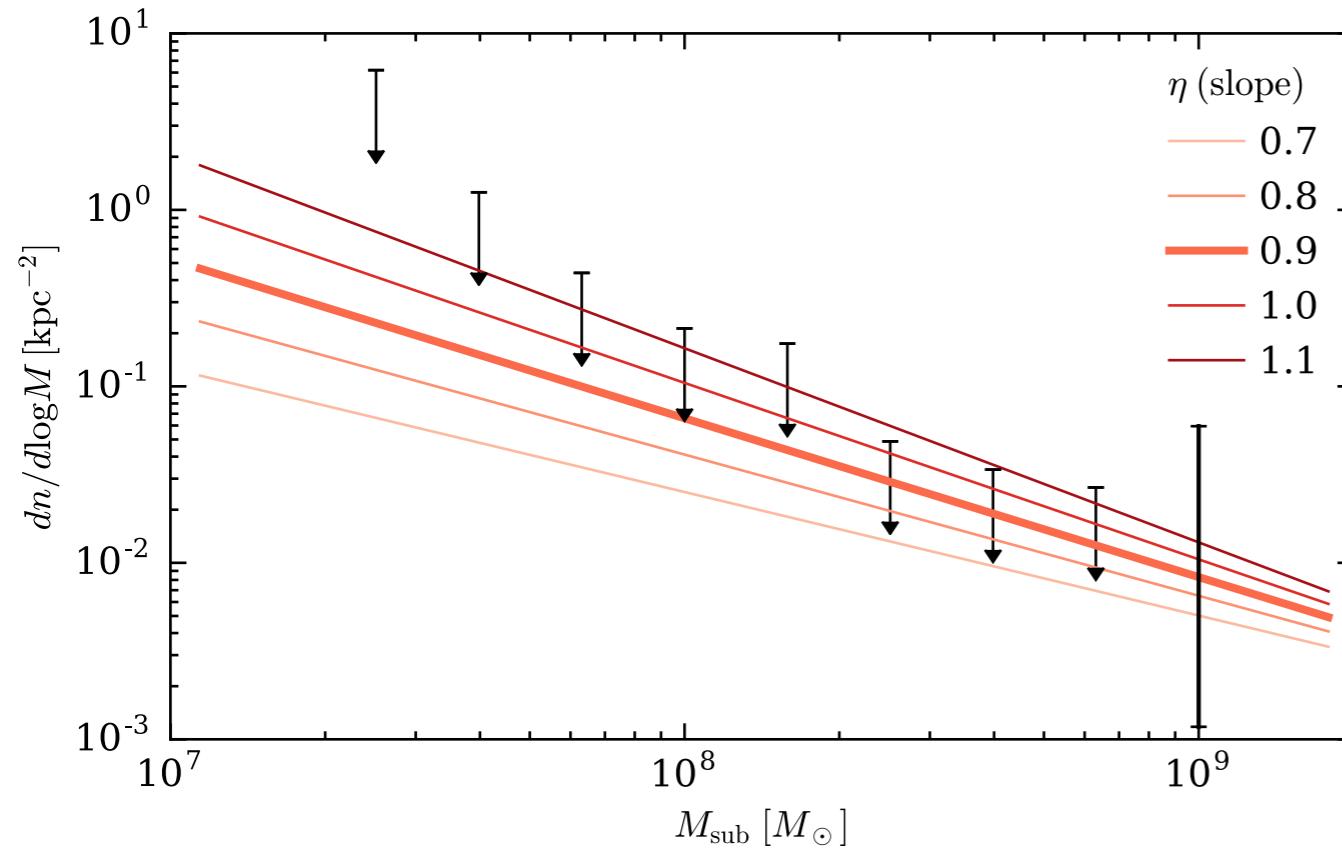
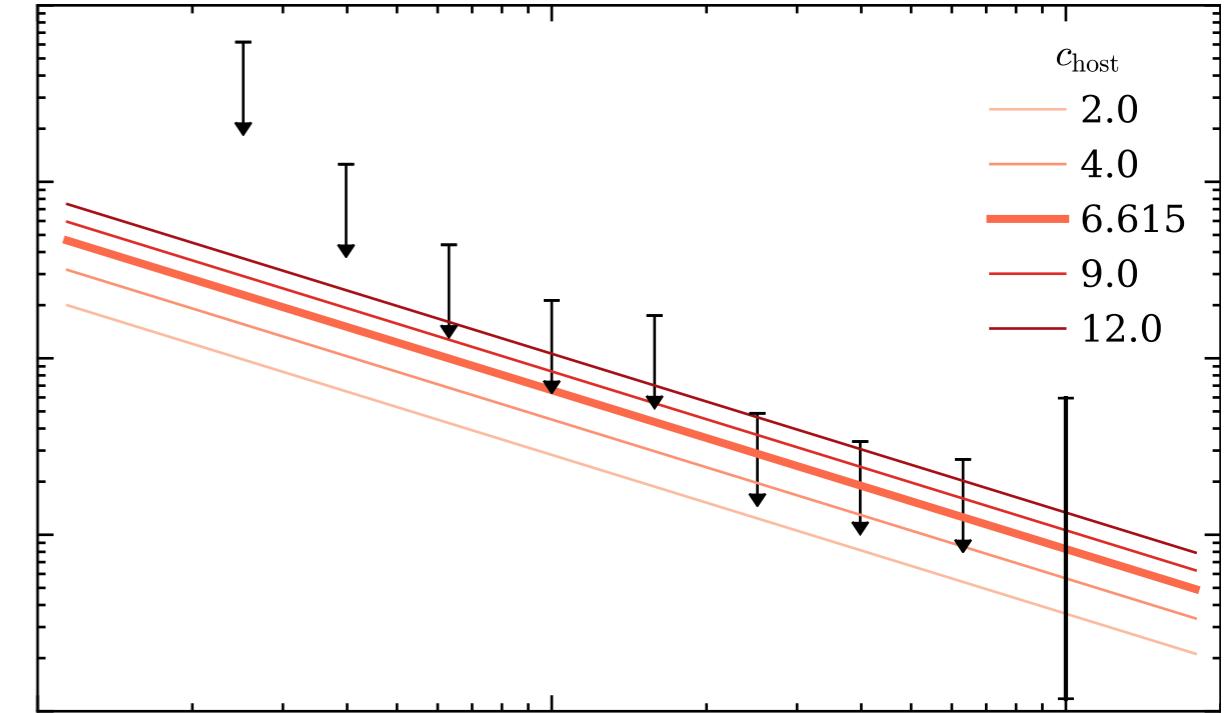
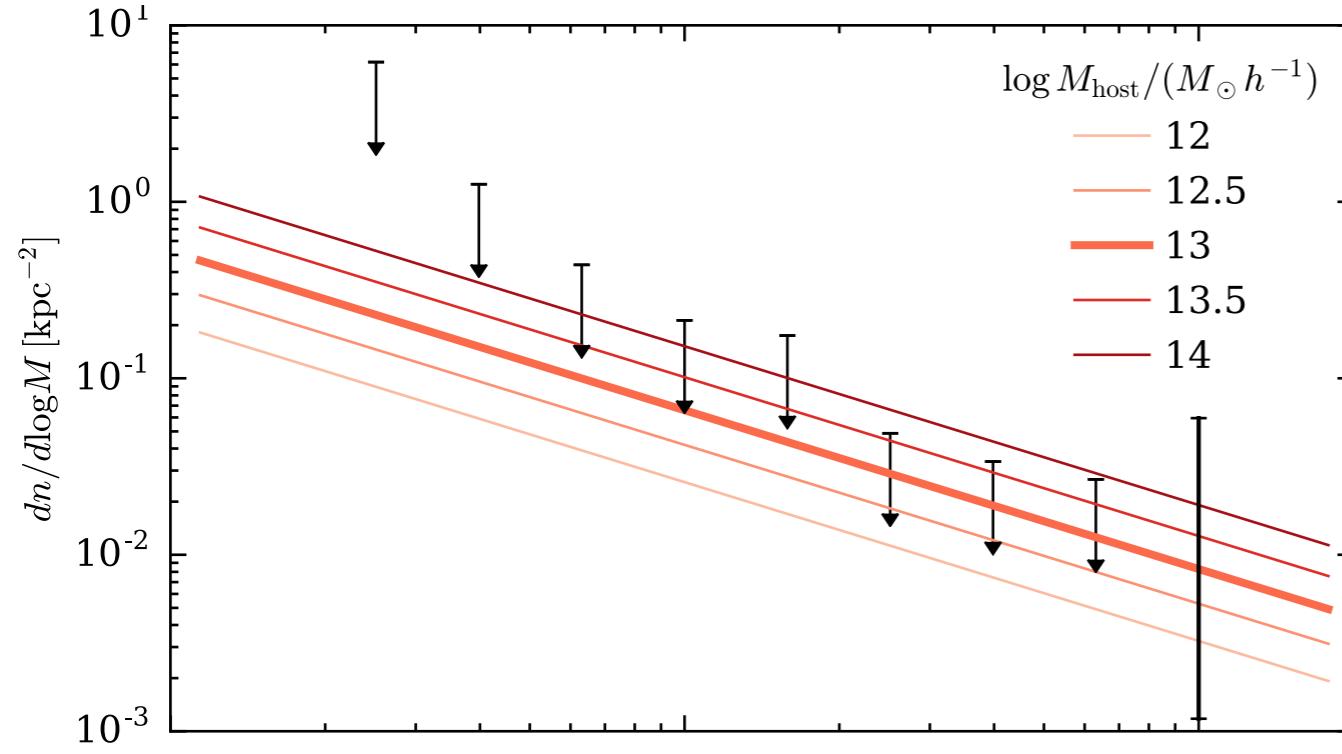
- this map shows how the fit improves ($\Delta\chi^2$) as we add a subhalo at various other locations...



- seems to be $\sim 4.5\sigma$ hint for an additional subhalo with $M=10^8 M_\odot$

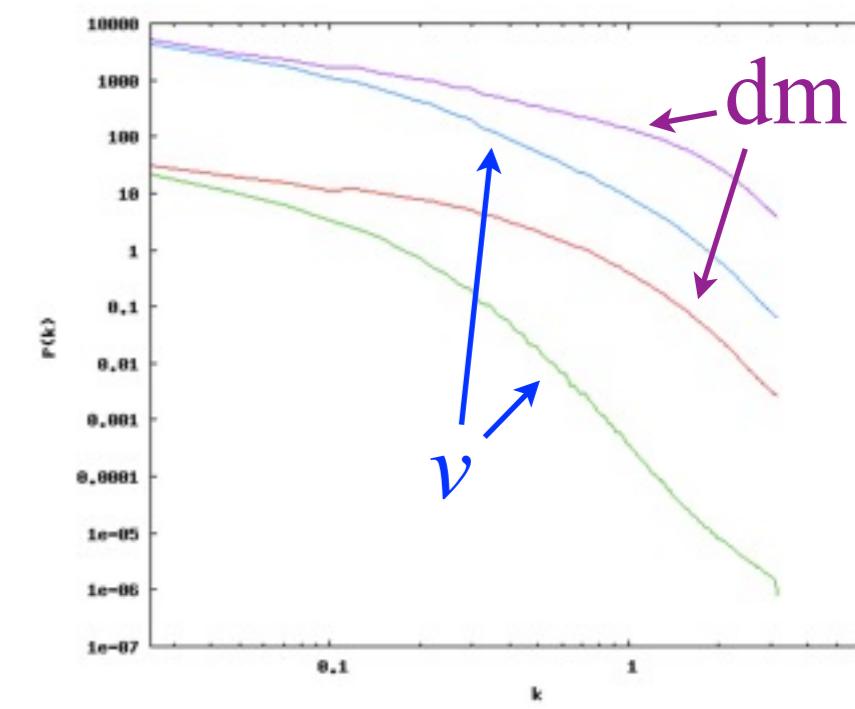
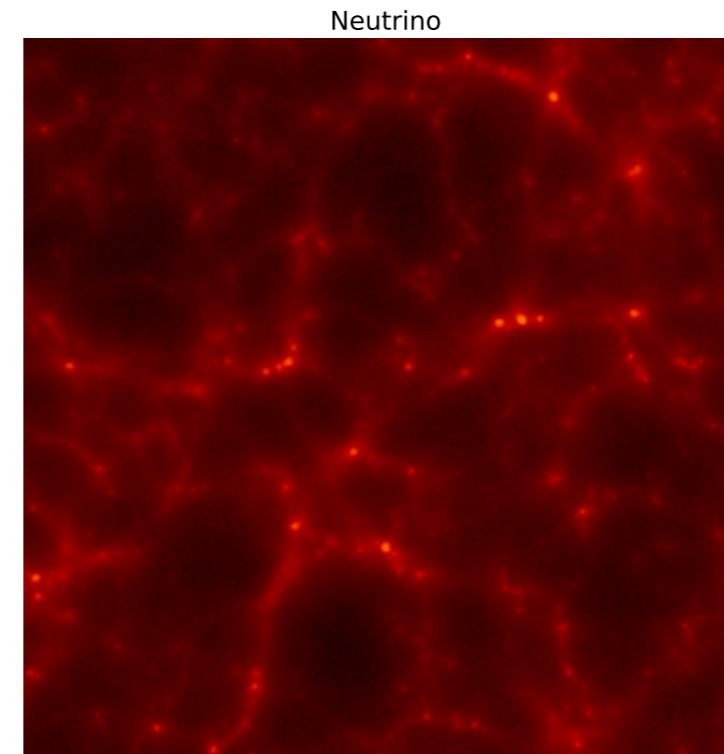
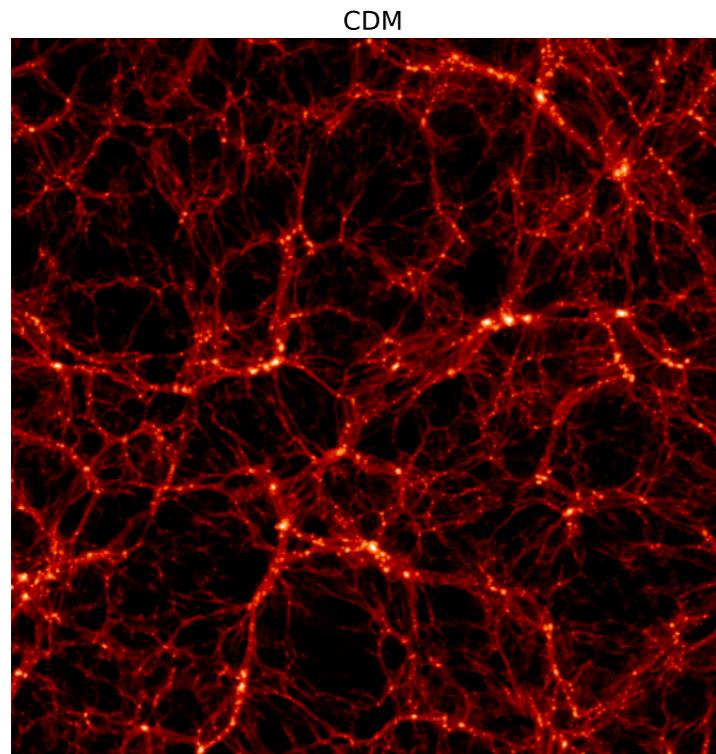
bounds on the subhalo mass function





New simulation code for hot particles

- with Arka Banerjee (student)
- combines elements of Lagrangian (N-body) and Eulerian (hydrodynamic) simulations
- applicable for WDM as well as massive neutrinos; avoid shot noise problems that arise in N-body sims



CDM

neutrinos

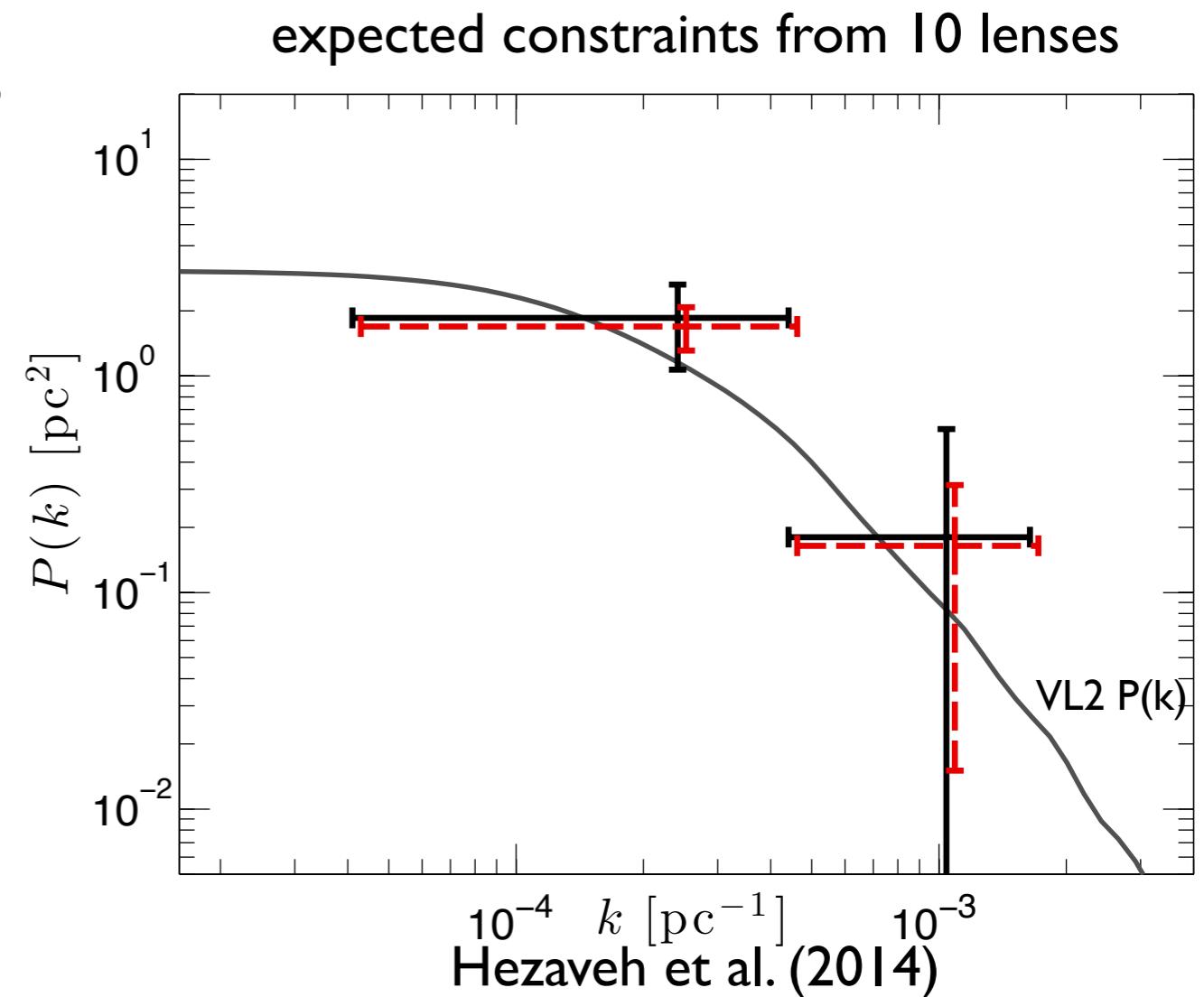
$P(k)$

Conclusion:

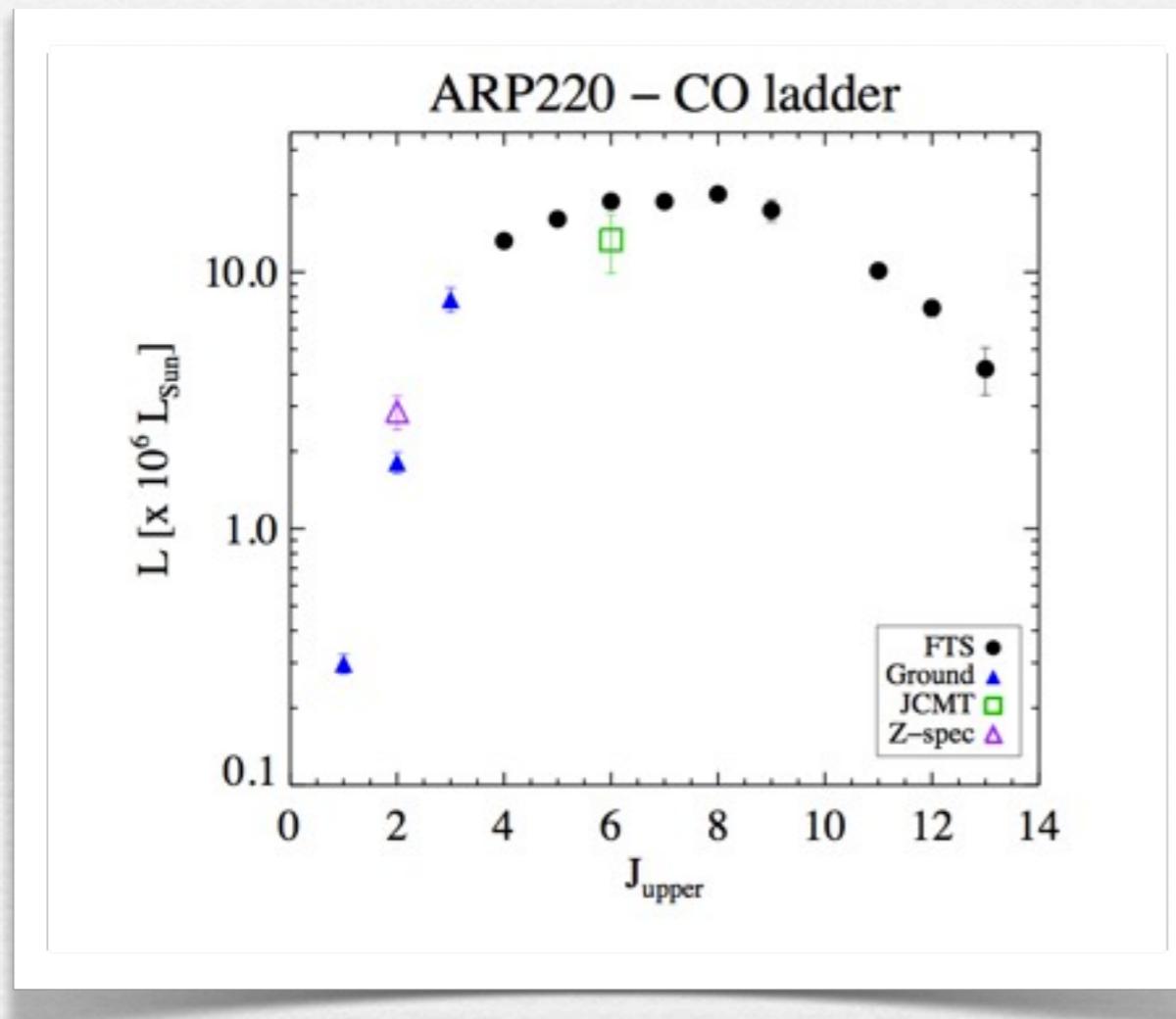
- SMG lensing is great for DM substructure
- stay tuned!

Substructure power spectrum

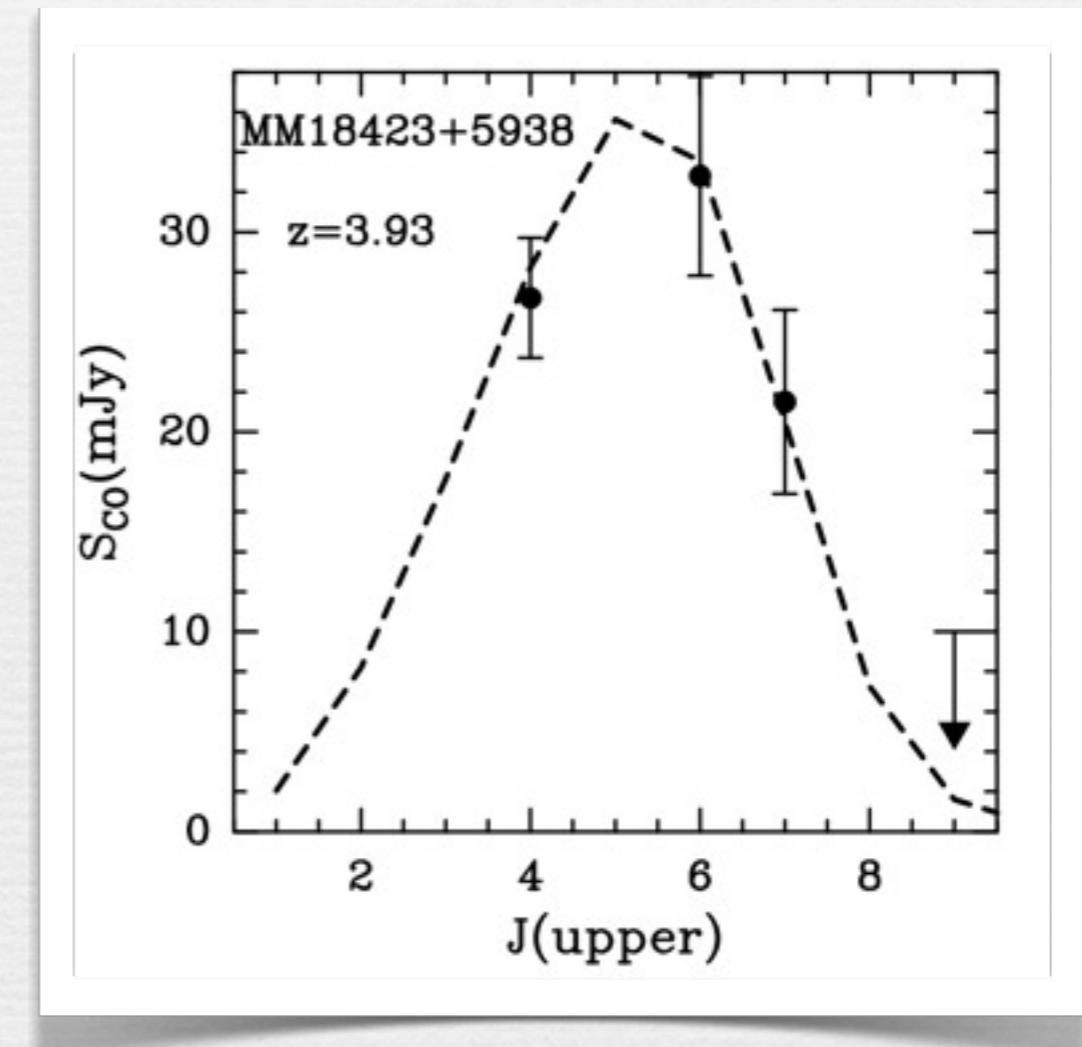
- besides all the big, $5-10\sigma$ objects, there are many more subhalos that produce $1-2\sigma$ effects.
- although we don't detect them individually, their **collective** effects can be detected
- note: easily distinguishable from measurement noise or source fluctuations



Strength of High-J Lines



RANGWALA ET AL 2011, APJ 743-1



LESTRADE ET AL 2010, A&A 522

⇒ High excitation lines are

- 1) more compact (more sensitivity to substructure)
- 2) brighter (higher signal to noise ratios)